

Brain Connectivity Overview

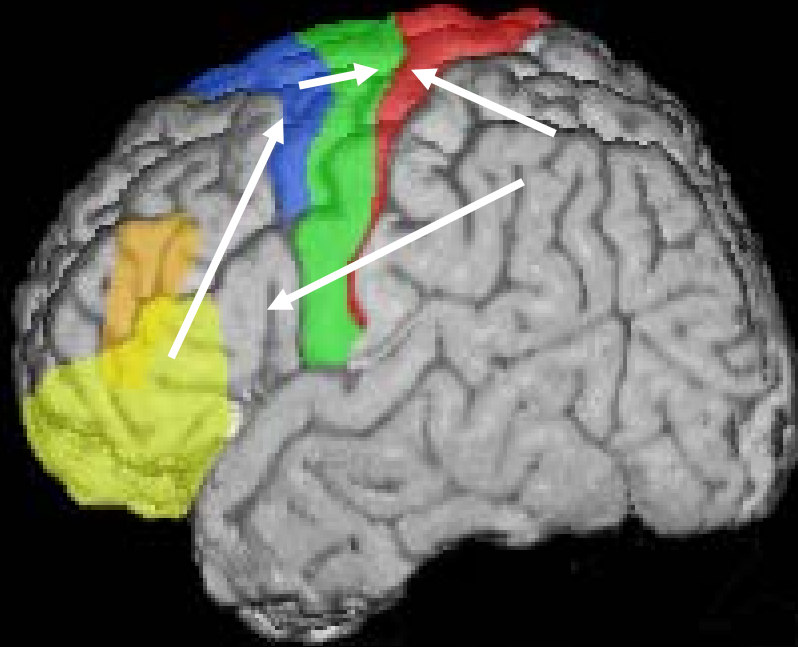
Thomas Zeffiro M.D. Ph.D.



- SPM 8/12
- ART Toolbox
- PPI
- GIFT
- DCM
- Connectivity Toolbox
- Brainwaver



regional specialization



regional interaction

Regional Interactions

```
graph TD; A[Regional Interactions] --> B[Functional connectivity]; A --> C[Effective connectivity];
```

Functional connectivity

= the temporal correlation between spatially remote areas

MODEL-FREE

Exploratory

Data Driven

No Causation

Whole brain connectivity

Effective connectivity

= the influence one area exerts over another

MODEL-DEPENDENT

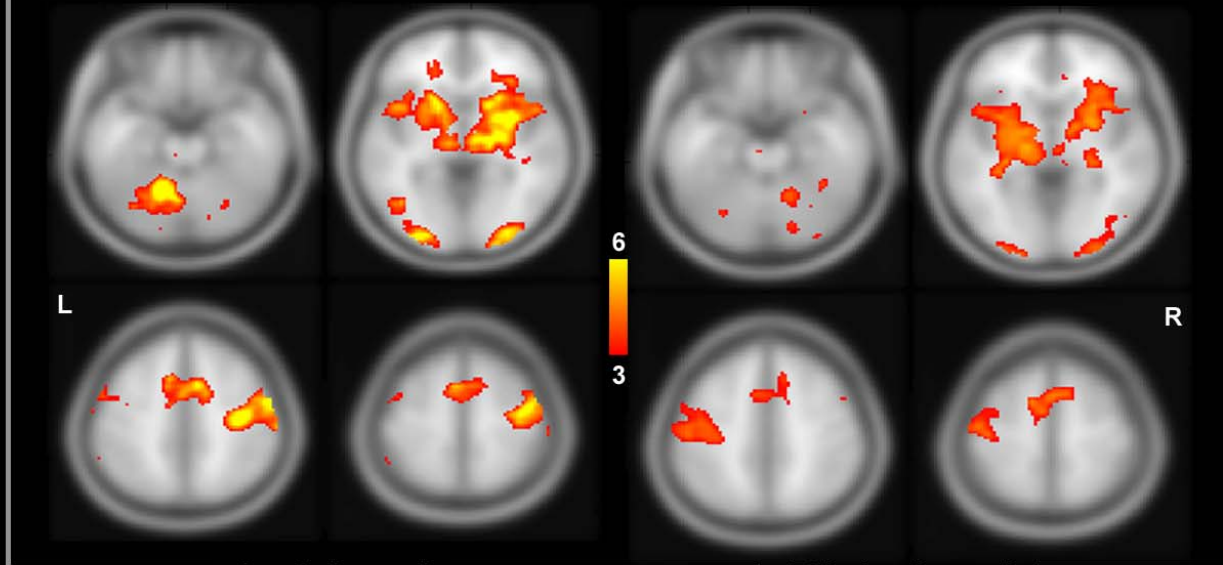
Confirmatory

Hypothesis driven

Causal

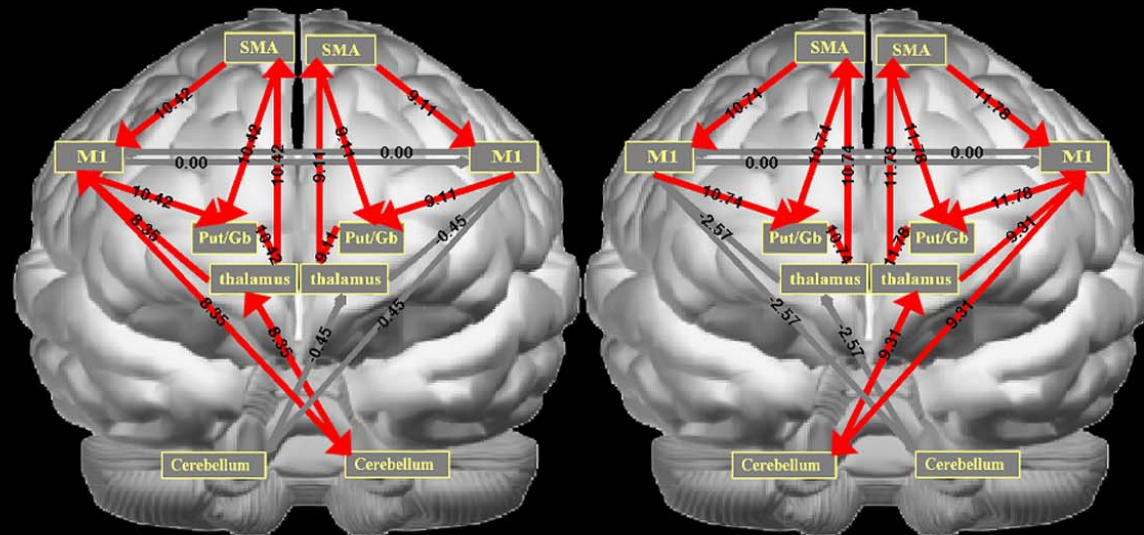
Reduced set of regions

Functional connectivity



Left hand

Right hand

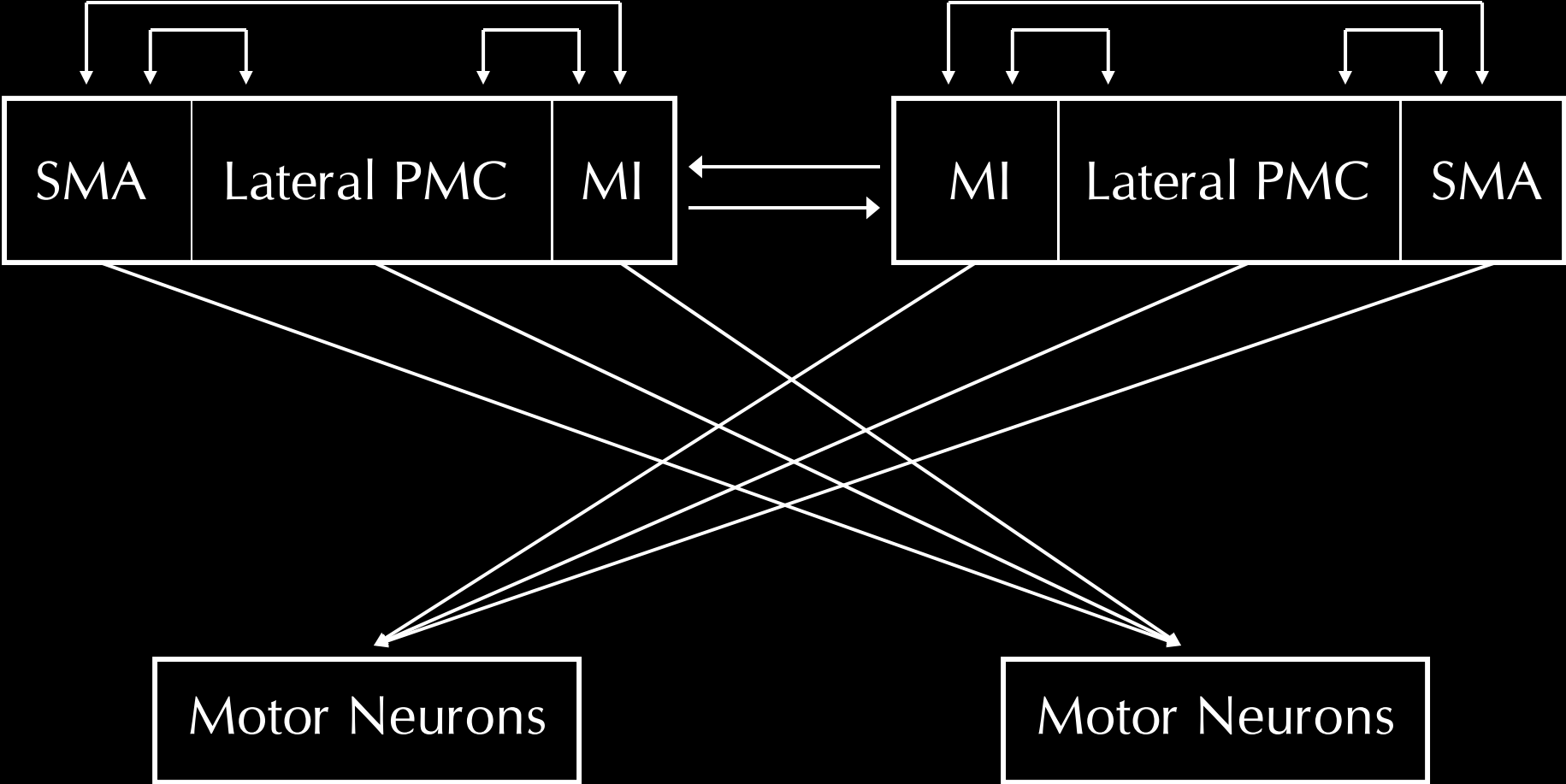


Effective connectivity

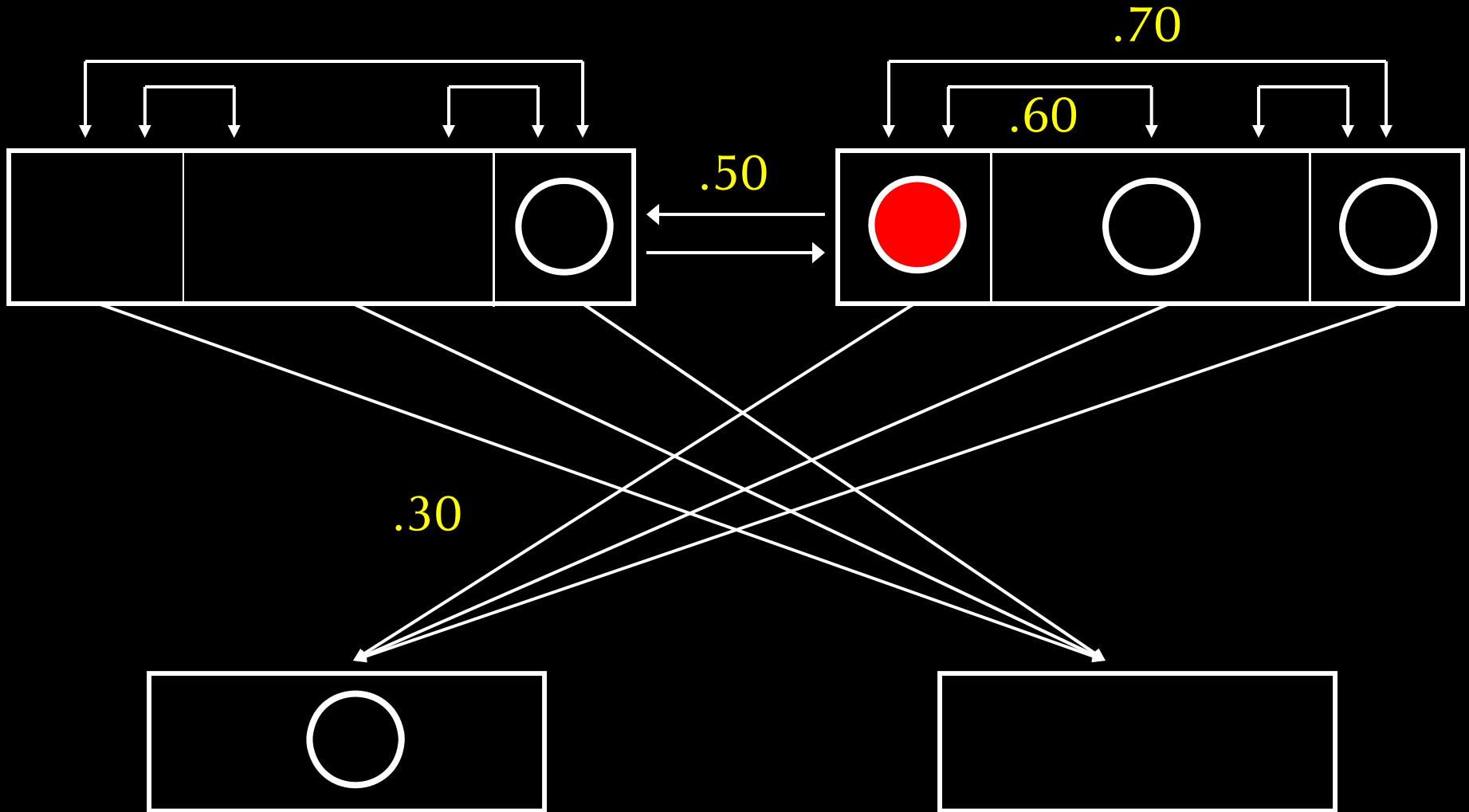
Regional Integration Modeling

- Functional connectivity
 - Bivariate correlation
 - Multivariate modeling (PCA, ICA, PLS)
- Effective connectivity
 - Psychophysiological interaction (PPI)
 - Mediation analysis
 - Structural equation modeling (SEM)
 - Multivariate autoregressive modeling (Granger causality)
 - Dynamic causal modeling (DCM)

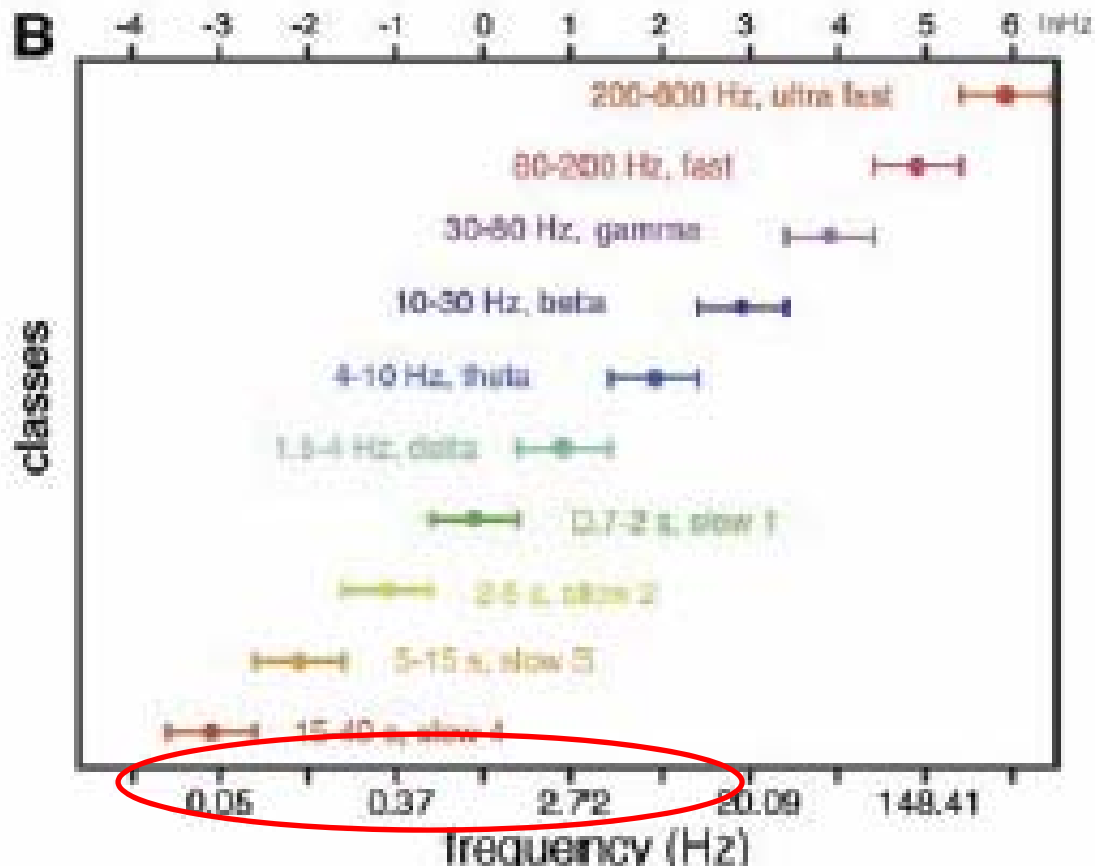
Motor System Horizontal Organization



Bivariate correlation



Information Frequency Bands



[.025 .06], toolbox cutoff [.009 .08]

Buzsaki , Science 2004

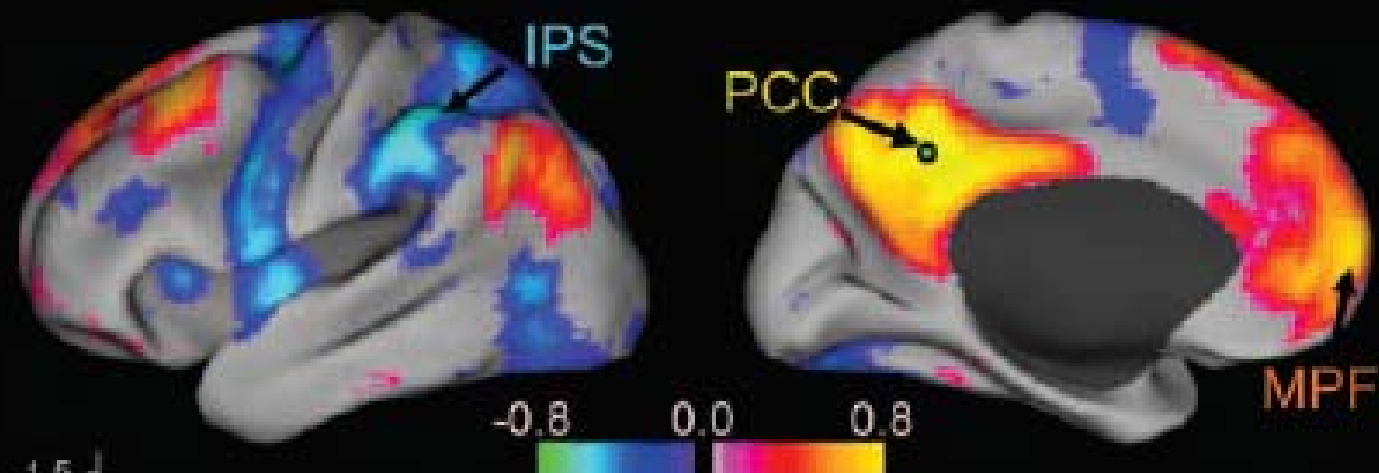
Resting State Networks

Spontaneous, low-frequency fluctuations in fMRI BOLD-contrast that form specific networks of the human brain in the absence of an overt task.

(Biswal 1995, Lowe 2000, Greicius 2003, Fox 2005)

Seed-driven functional connectivity

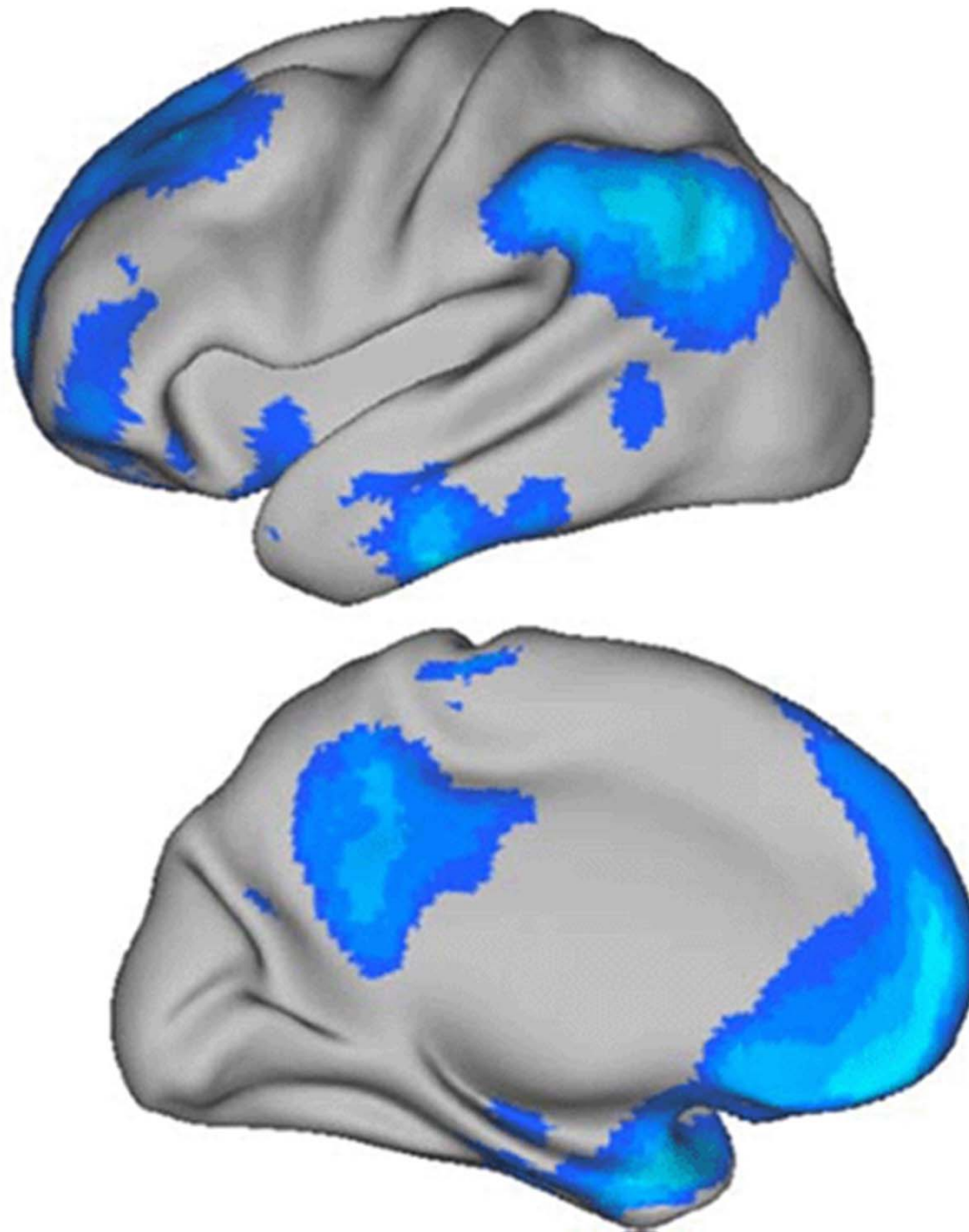
Estimate maps showing temporal correlations between the BOLD-contrast signal from a given seed and every other brain voxel

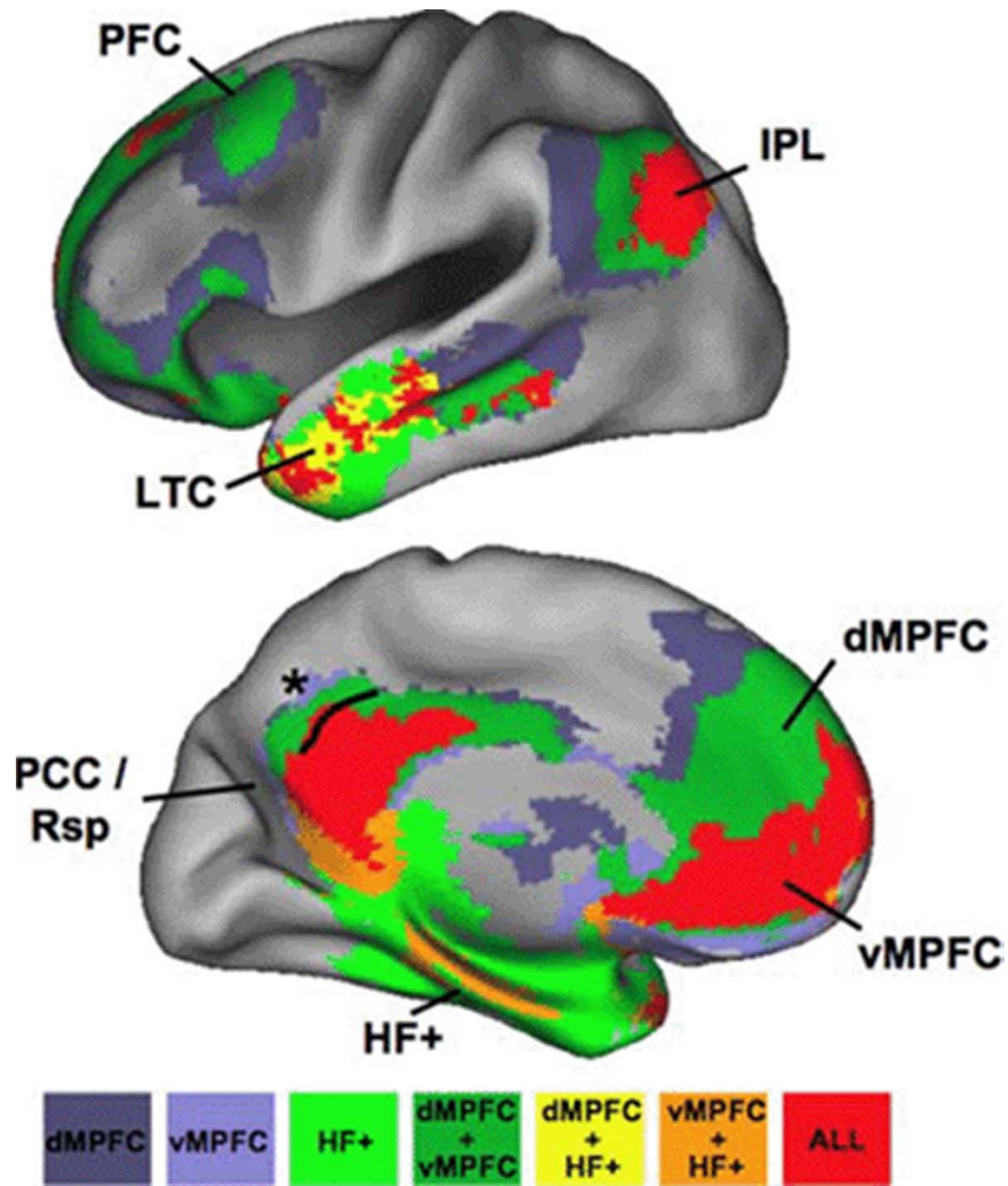


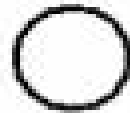
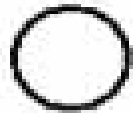
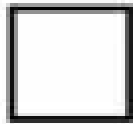
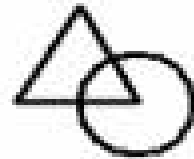
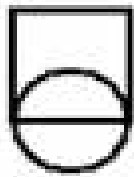
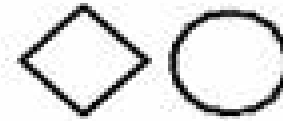
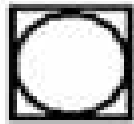
Fox et al., 2005. Proc. Natl. Acad. Sci. 102:9673–9678

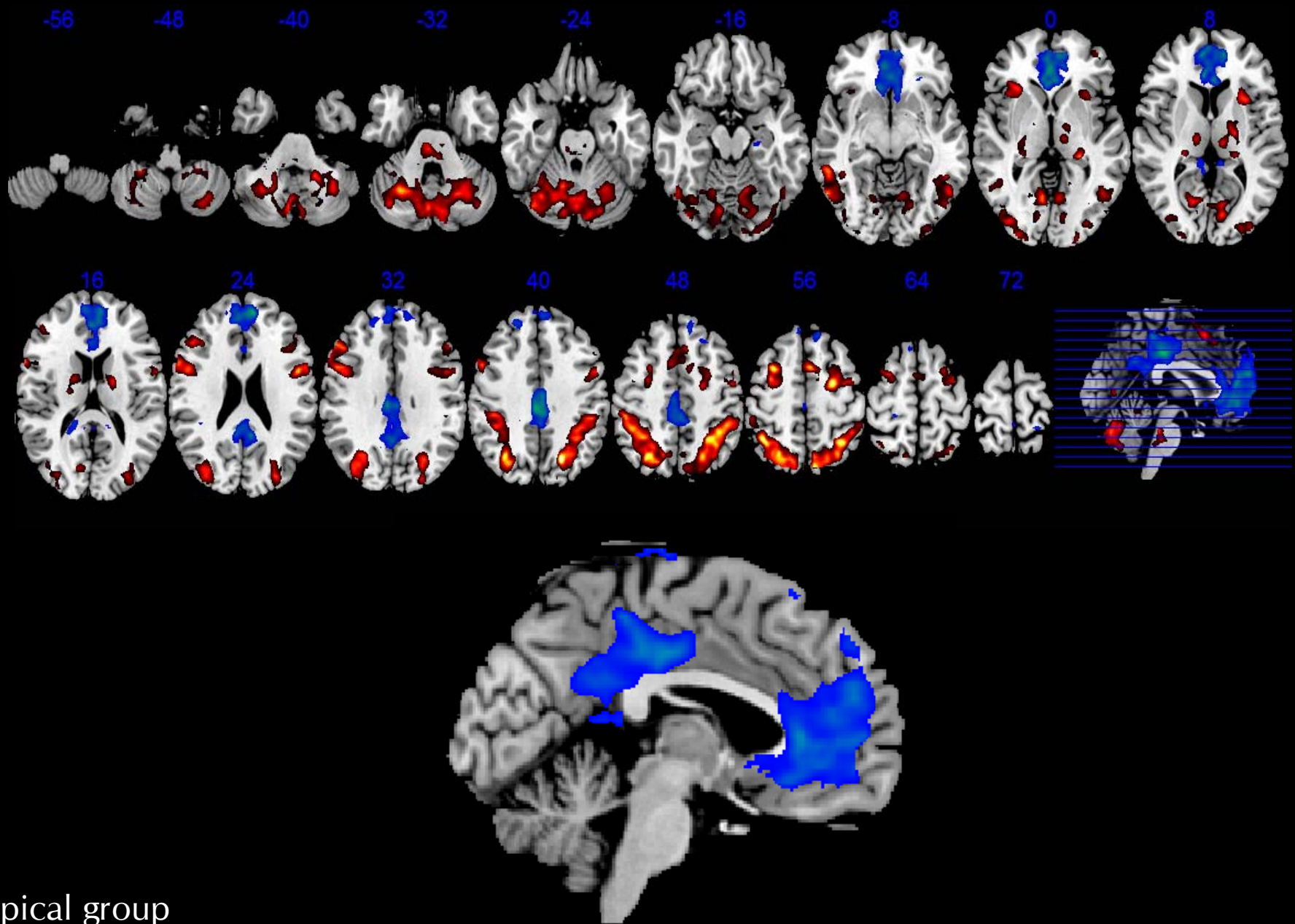
Vincent et al, 2006 J Neurophysiol 96:3517–3531

Whitfield-Gabrieli et al, 2009, Proc. Natl. Acad. Sci. 102:9673–9678









Typical group
N = 17

Noise in connectivity analyses

Non-neuronal contributions to the BOLD-contrast signal

Noise sources

Physiological noise
Scanner drift
Subject motion

In “activation” studies

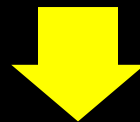
Nuisance effects

Usually degrade power (lower statistical significance of the results)

In “connectivity” studies

Confounding effects

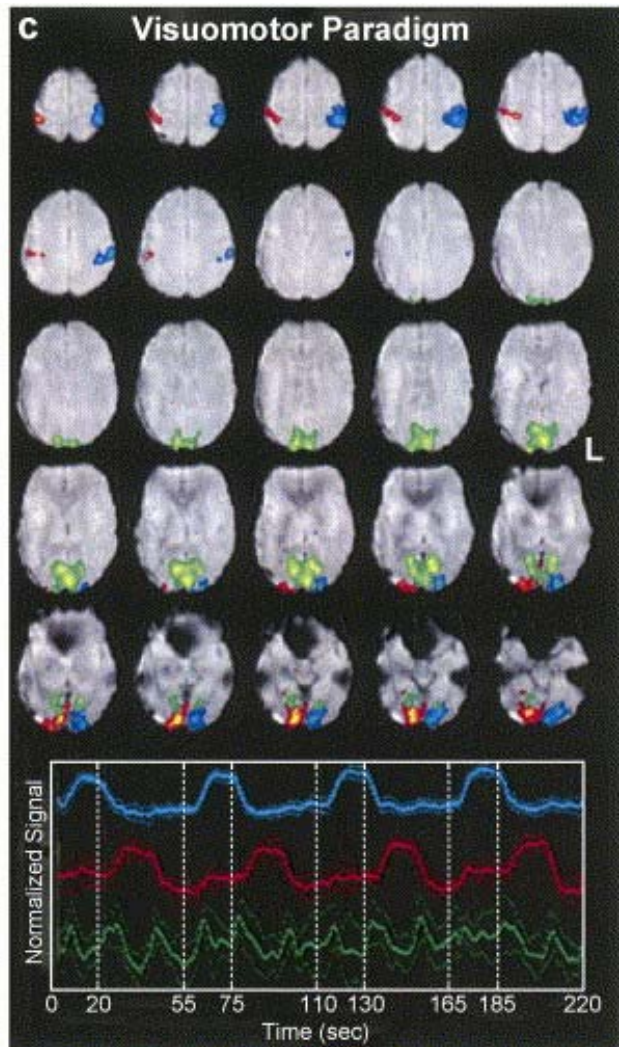
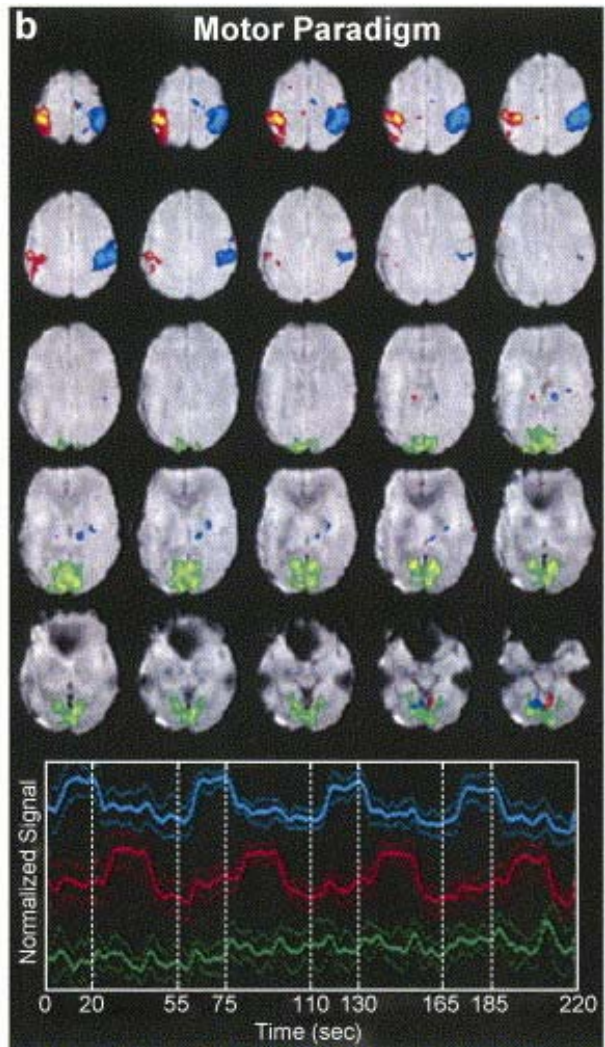
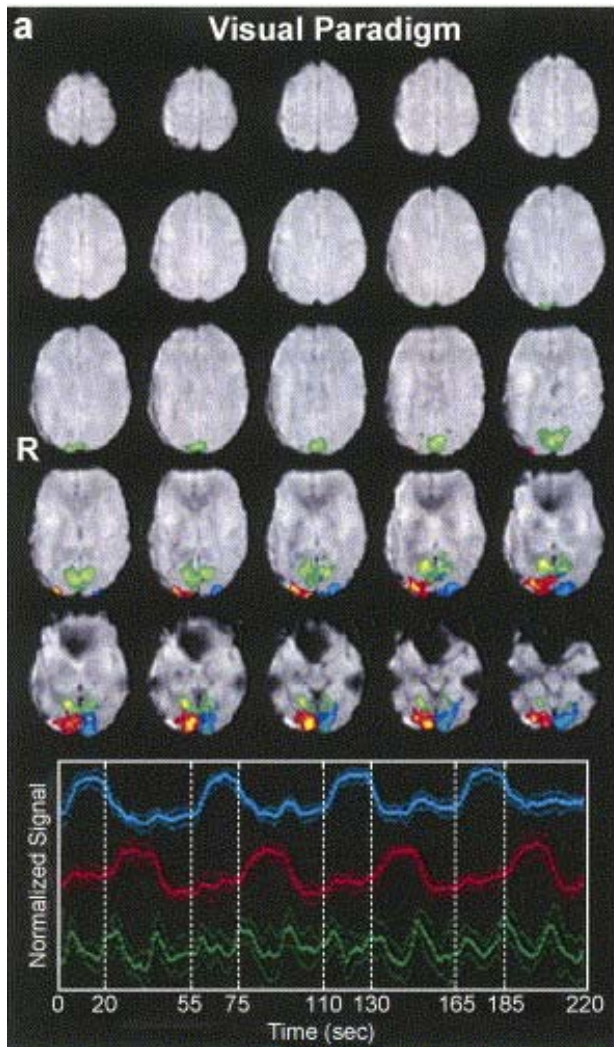
Introduce bias in results (show apparent connectivity between unrelated areas)



Need to appropriately characterize and remove noise effects to improve the validity of connectivity analyses

Regional Integration Modeling

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Independent Component Analysis

- A blind source separation (BSS) method
- Goal: separate sources from a linear mixture
- Model: $\mathbf{X}=\mathbf{AS}$
 - \mathbf{X} : Mixture (observed data)
 - \mathbf{A} : Mixing coefficients (estimated)
 - \mathbf{S} : Sources (estimated)
- Estimate: $\hat{\mathbf{S}} = \mathbf{WX}$, $\mathbf{W} = \mathbf{A}^{-1}$, based on maximizing statistical independence of $\hat{\mathbf{S}}$
- Assumptions
 - Linear mixing
 - Independence of sources
 - Non-Gaussian sources

a (not so scary) example

Observations (X)



=

$$X=AS$$

background



Mixing matrix (A)

candle 1



candle 2

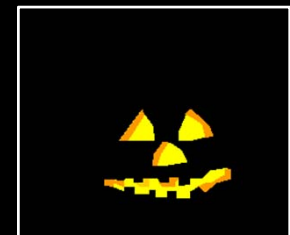
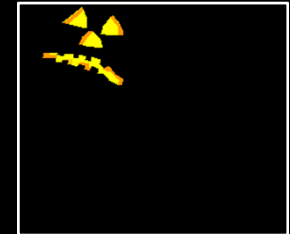


candle 3



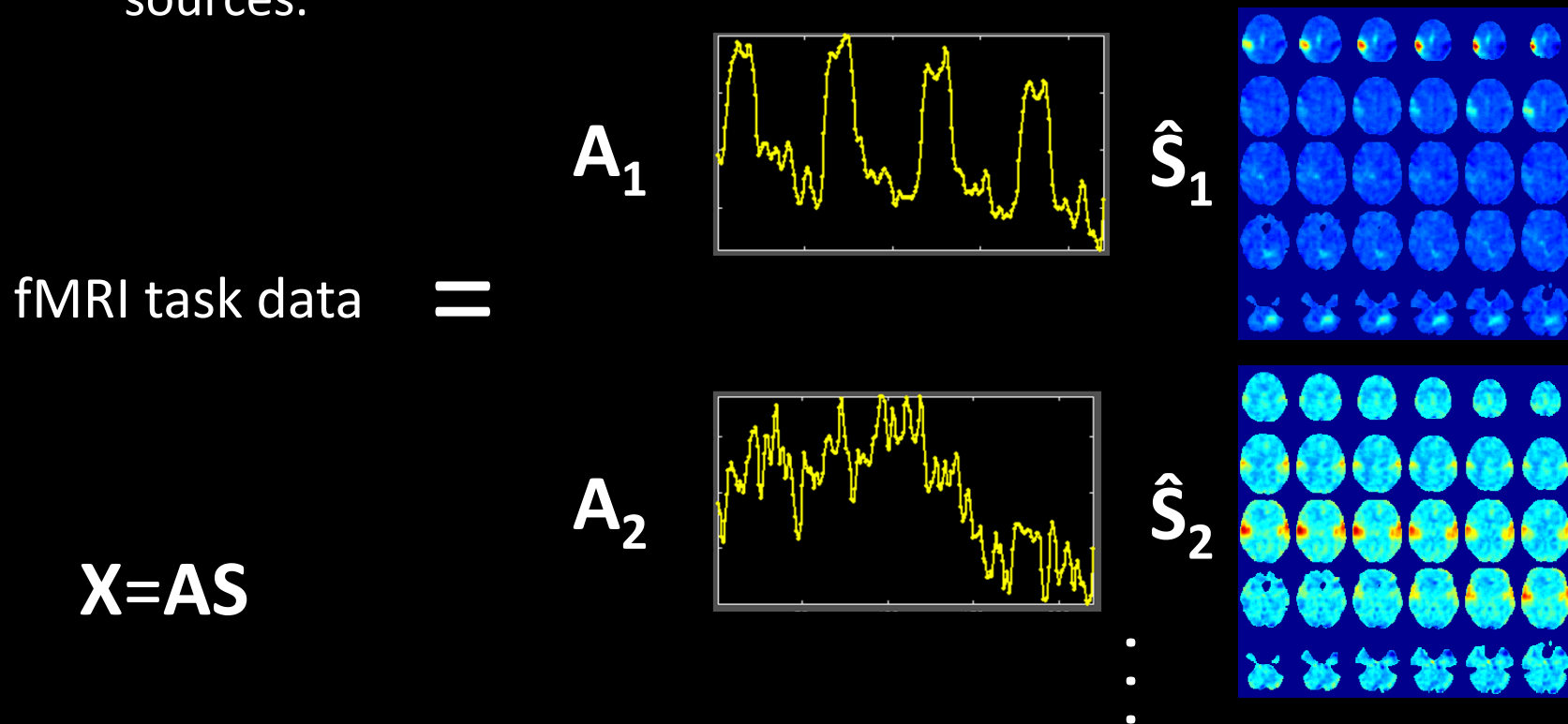
time candle out

Sources (S)



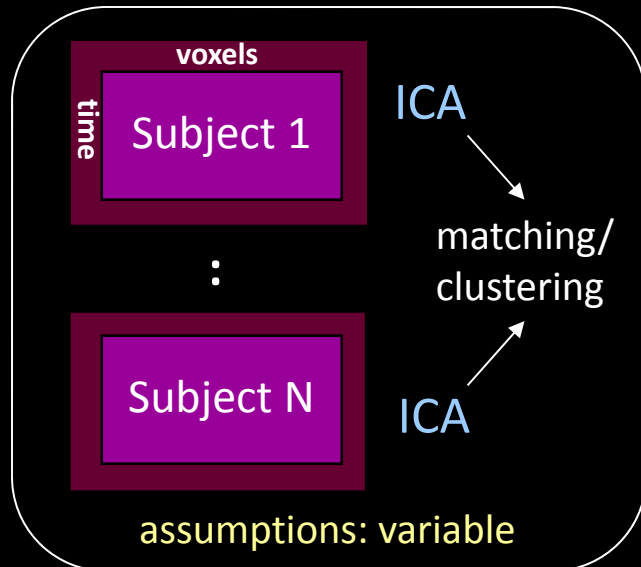
ICA applied to fMRI

- We typically perform spatial ICA:
 - the sources are maps that are **maximally spatially independent** (i.e., non-overlapping)
 - the mixing matrix represents **activation time courses** of the sources.

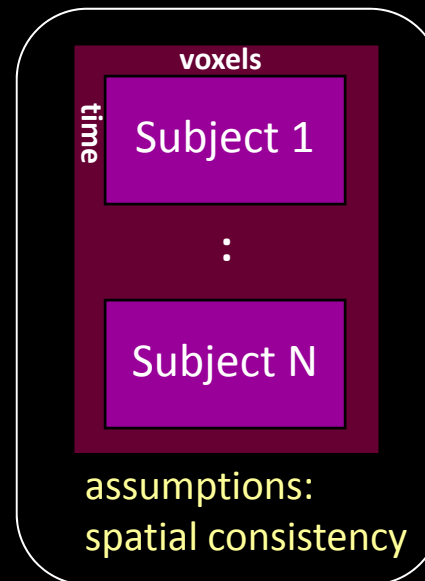


multi-subject ICA frameworks

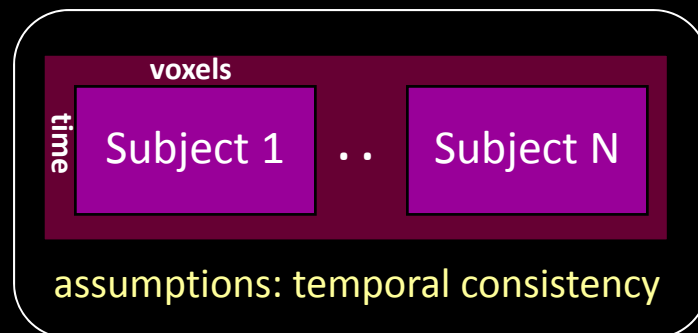
combine single subject ICAs



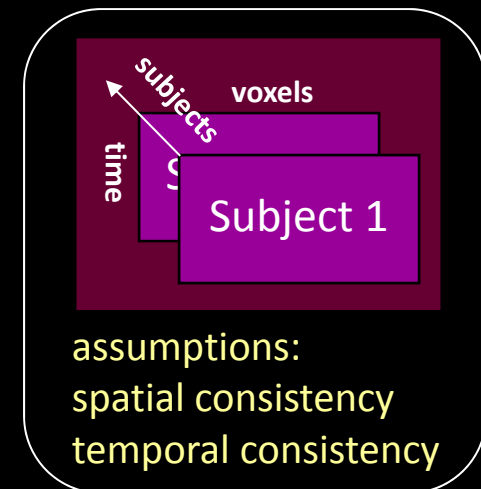
group ICA with
temporal concatenation



group ICA with spatial concatenation

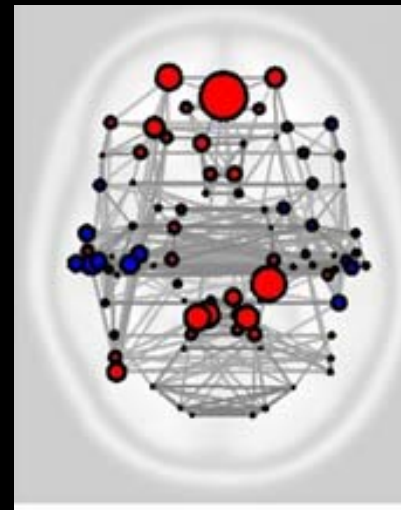
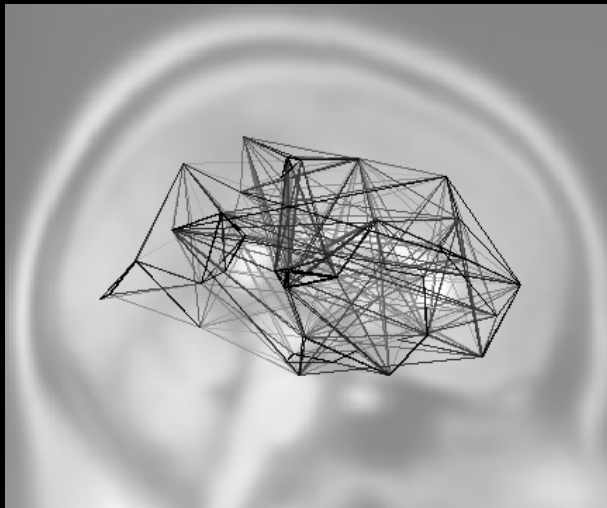


tensor ICA

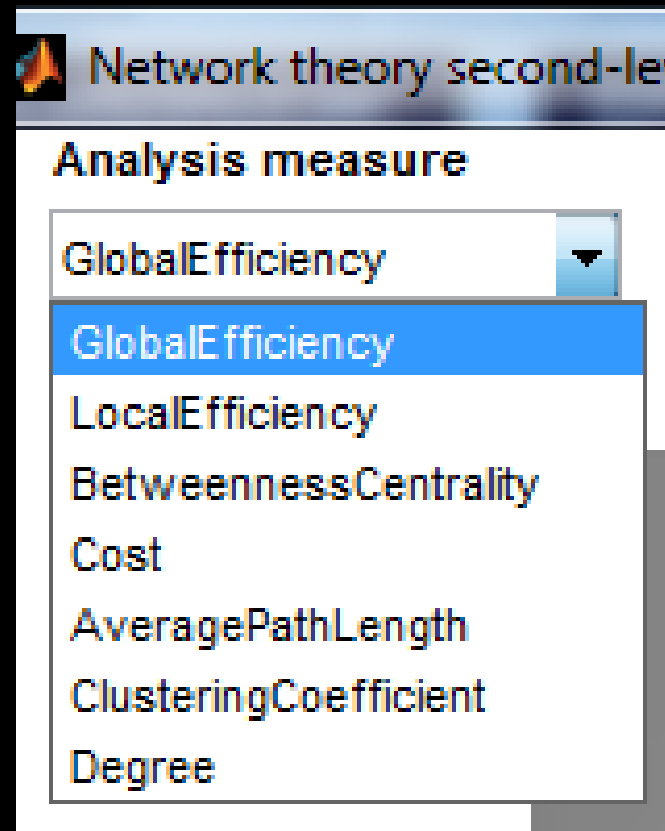


Graph-theory analyses

- **ROI-to-ROI connectivity matrices provide a framework to investigate functional architecture and network topology with graph theoretic analyses.**



Graph-theory analyses



The image shows a software window titled "Network theory second-le". Below the title bar is a section labeled "Analysis measure". A dropdown menu is open, showing a list of analysis measures. The first item, "GlobalEfficiency", is highlighted in blue. The other items in the list are "LocalEfficiency", "BetweennessCentrality", "Cost", "AveragePathLength", "ClusteringCoefficient", and "Degree".

Network theory second-le

Analysis measure

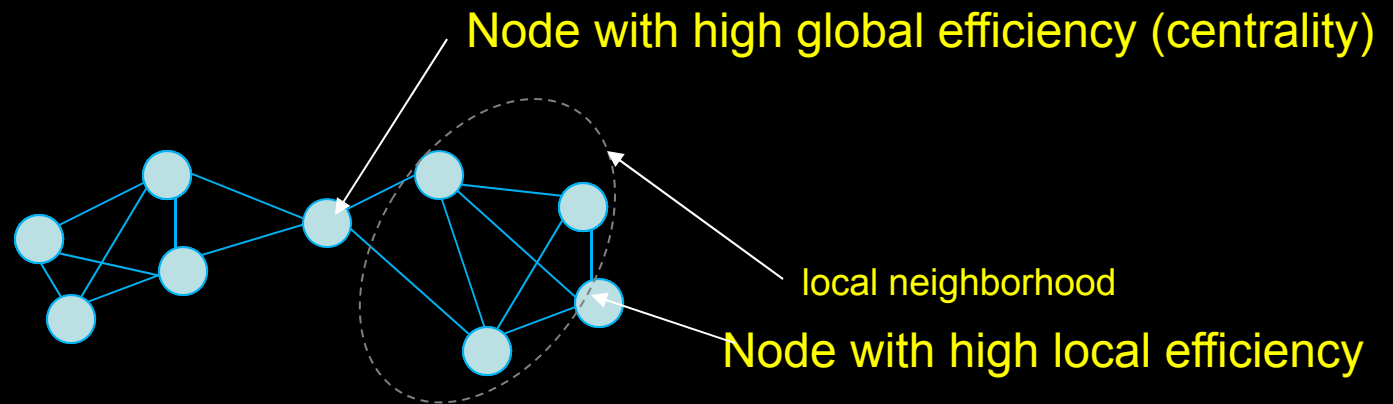
- GlobalEfficiency
- LocalEfficiency
- BetweennessCentrality
- Cost
- AveragePathLength
- ClusteringCoefficient
- Degree

Graph theory

- Properties of each ROI's contribution to the network:

Global efficiency: Average inverse distance (number of steps) in the shortest-path between one region and each of the other regions.

Measures the relative importance / centrality of a node in a network.



Local efficiency: Average inverse distance among all of the regions connected to a given region (dotted line in the example above).

Measures the 'locality' on an ROI (strength of the local network of connected ROIs)

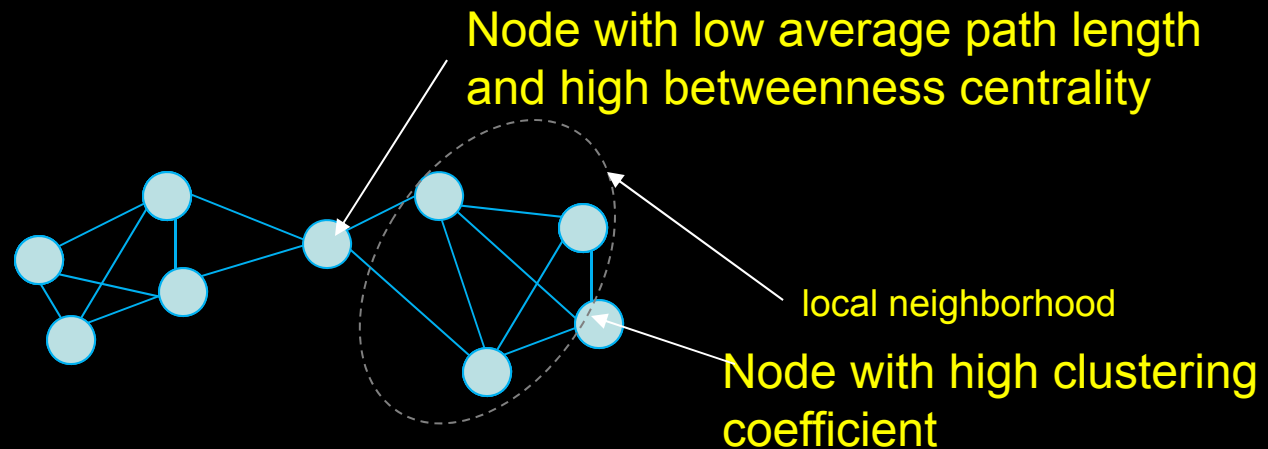
Node: Global & Local Efficiency

- High '*global efficiency*' for a node means that this node is 'closer' to all of the other nodes (it is also interpreted as a measure of 'centrality')
- High '*local efficiency*' for a node means that its neighbors are well connected to each other

Graph theory

Average path length: Average distance between a node and the rest of the nodes (inversely related to global efficiency)

Betweenness centrality: Proportion of all shortest-paths in the network (between all pairs of nodes) containing a given node



Cluster coefficient: Proportion of connected nodes in the local graph containing only the neighbors of each node (related to local efficiency)

Cost/degree: Proportion/number of regions connected to a given region

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Psycho-physiological Interaction (PPI)

- Measure of functional connectivity, and how it is affected by psychological variables
- Looks at how brain activity can be explained by the interaction between 2 variables
 - an experimental variable (e.g. level of attention)
 - activity in a particular brain area (source area)
- This is done voxel-by-voxel across the entire brain

PPIs vs typical interactions

		Task	
		Attend eyes	Attend mouth
Stimulus	Upright face	$T_1 S_1$	$T_2 S_1$
	Inverted face	$T_1 S_2$	$T_2 S_2$

PPIs vs typical interactions

- A typical interaction
 - Use General Linear Model:

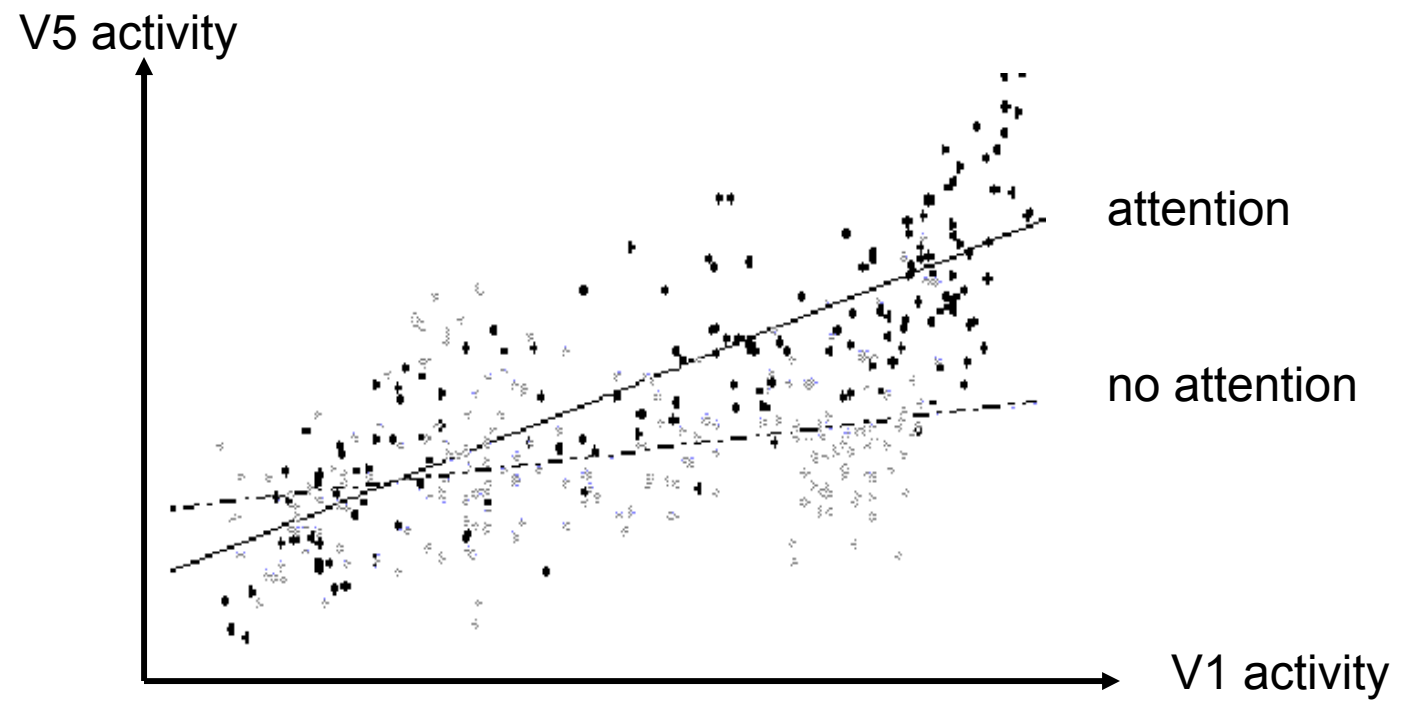
$$Y = (T_1 - T_2) \beta_1 + (S_1 - S_2) \beta_2 + (T_1 - T_2)(S_1 - S_2) \beta_3 + e$$

- A PPI
 - Replace one of the variables with activity in source region
 - Eg for source region V1:

$$Y = (T_1 - T_2) \beta_1 + \mathbf{V1} \beta_2 + (T_1 - T_2)\mathbf{V1}\beta_3 + e$$

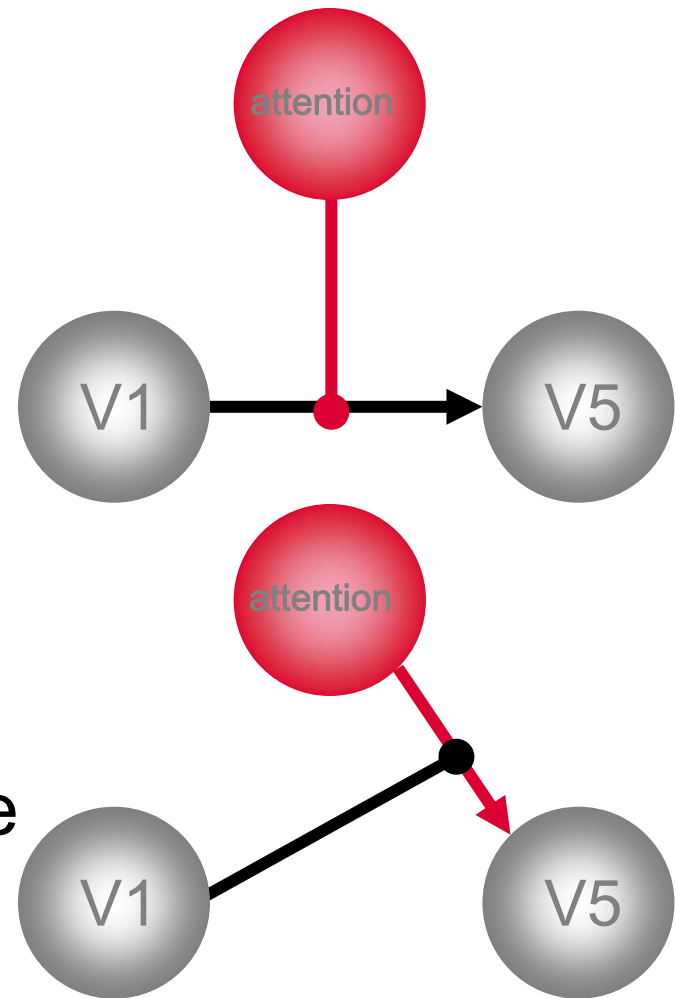
PPI – an example

- Investigating influence of 2 factors:
 - V1 activity
 - AttentionOn activity in region V5
- Measure brain activity under 2 conditions of attention



Interpreting PPI

- 2 possible ways:
 - Contribution of source area to target area (ie the effective connectivity) depends on experimental context
 - Response of target area to experimental variable depends on activity of source area
- Mathematically, both are equivalent, but one may be more neurologically plausible



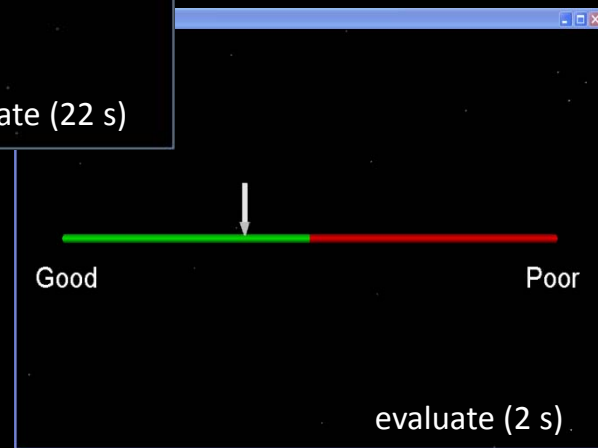
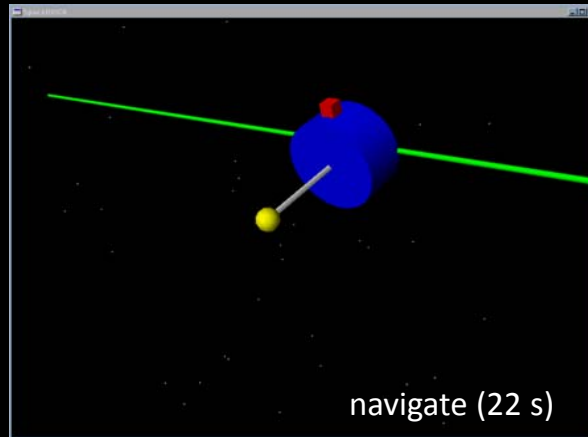
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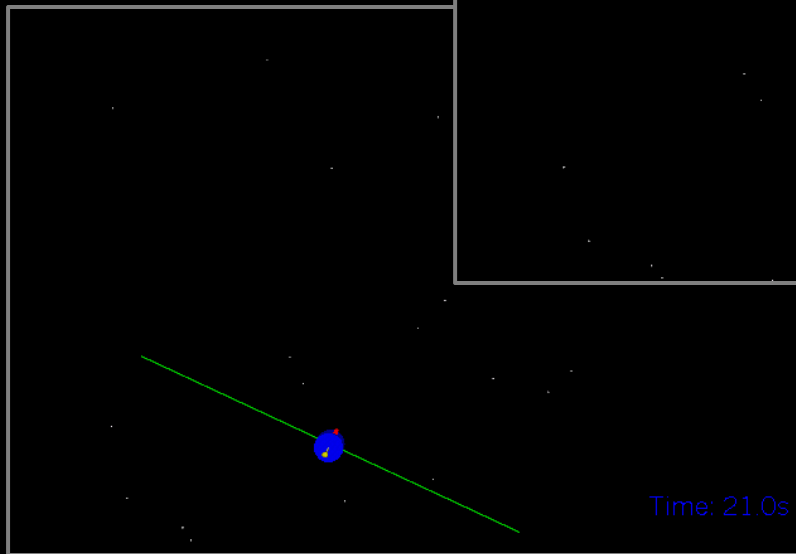
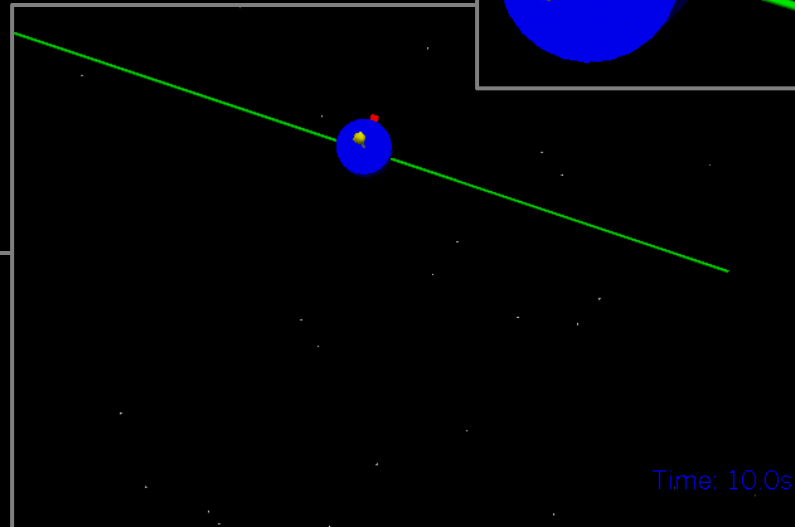
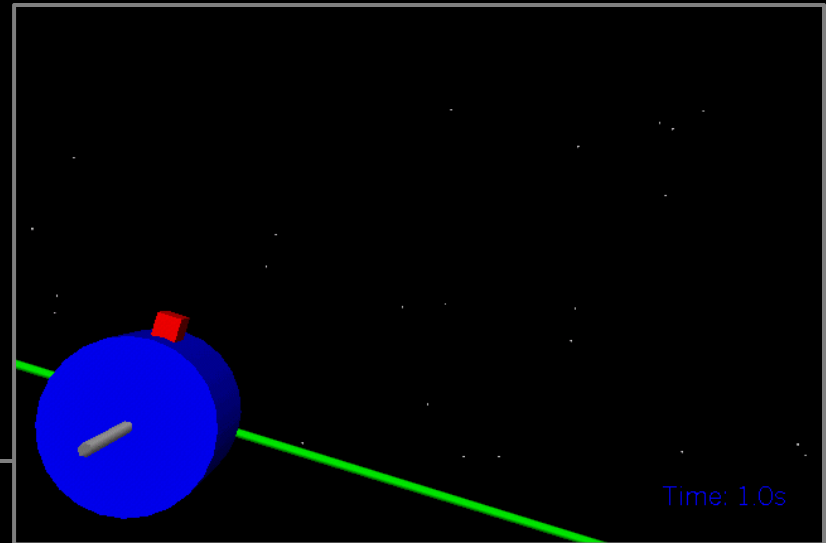
Simulated
target



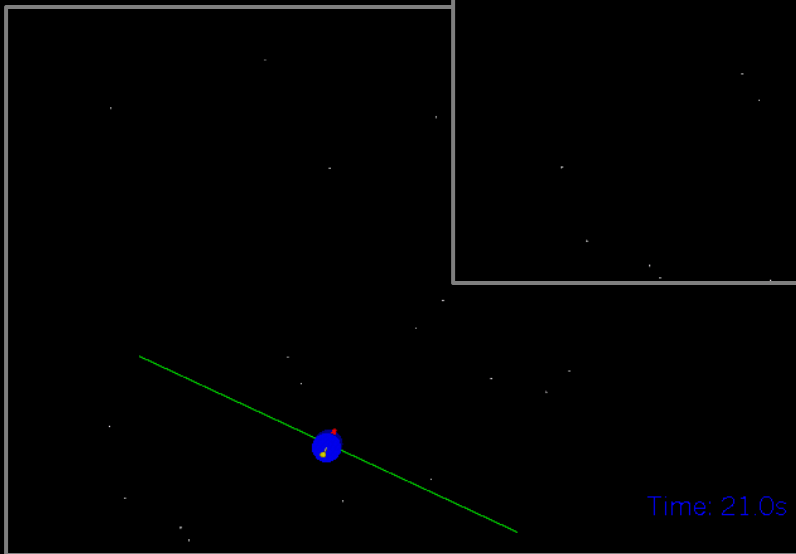
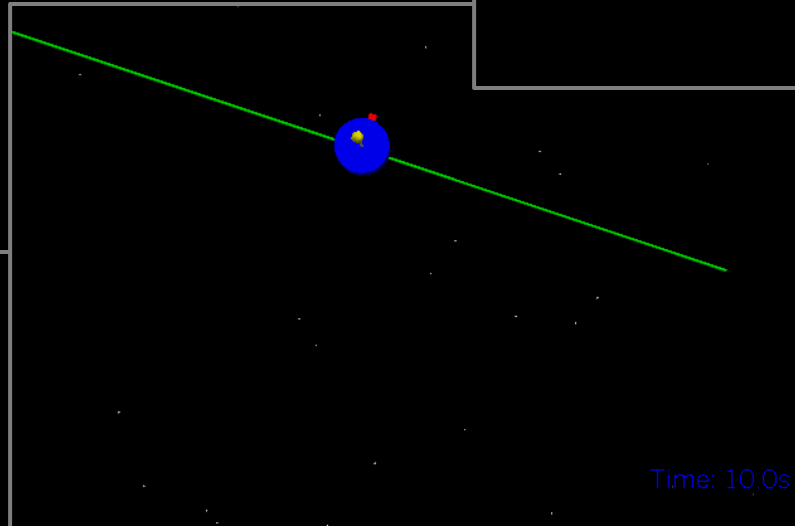
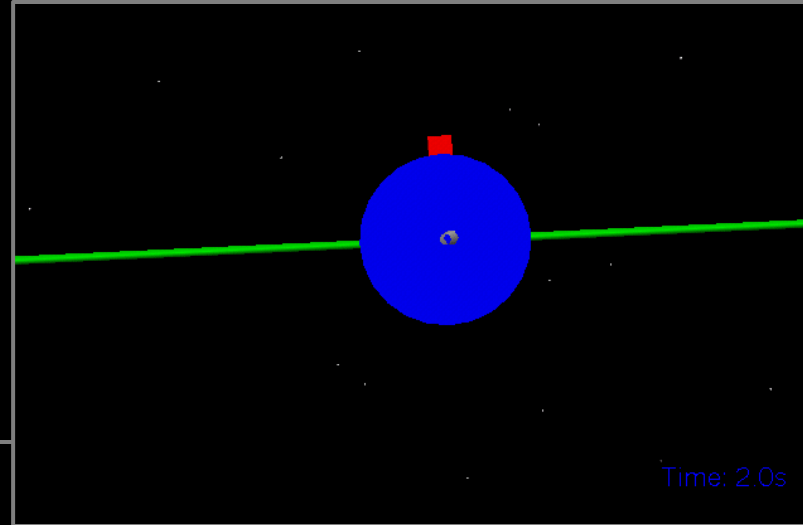
Joystick navigation



miss

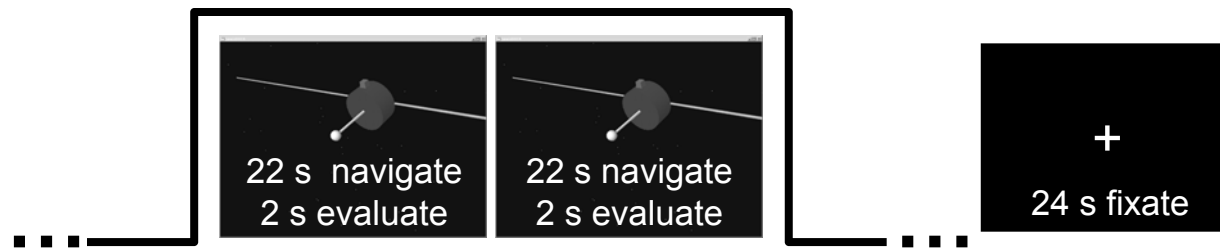
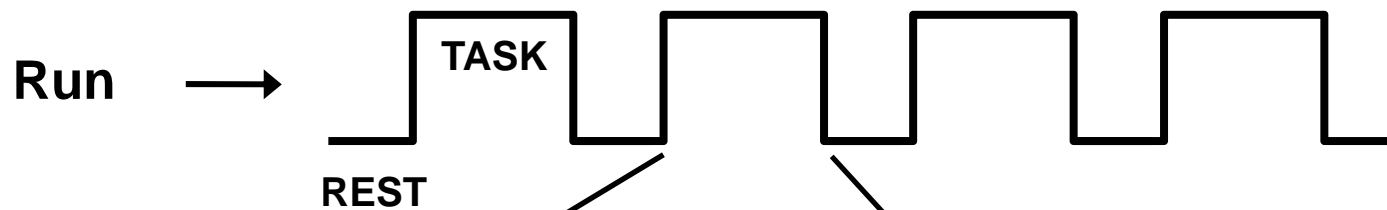


hit



Experiment timing

Number of MR Volumes → 12 24 12 24 12 24 12 24 12



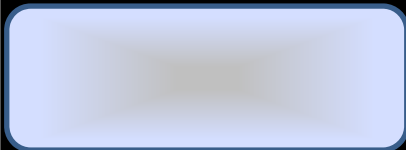

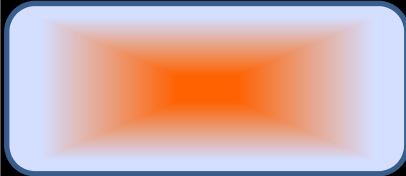

Run length 5.2 min

Five runs per session

Experiment factorial design

TASK

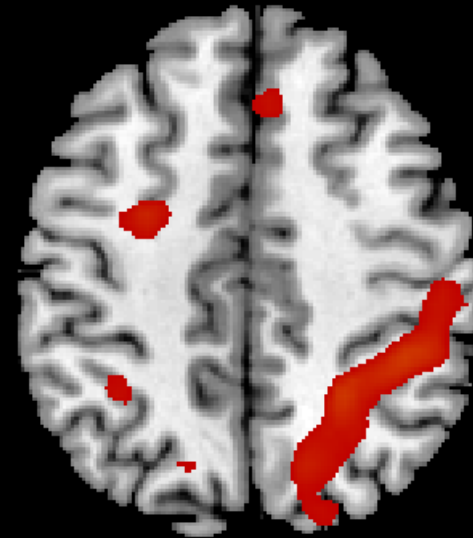
SLEEP

	navigate	evaluate
normal		
deprived		

Navigate

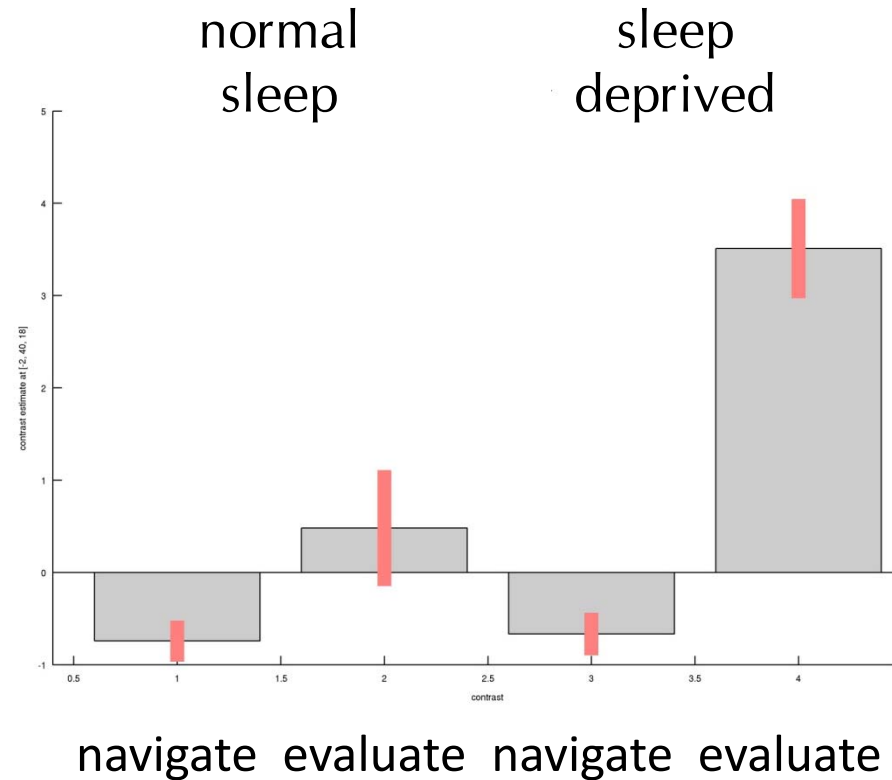
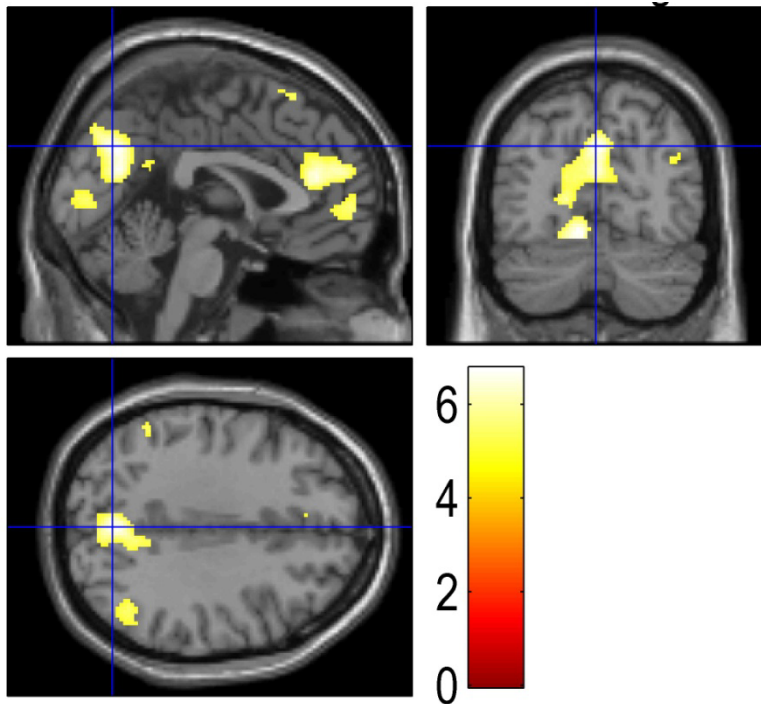


Evaluate



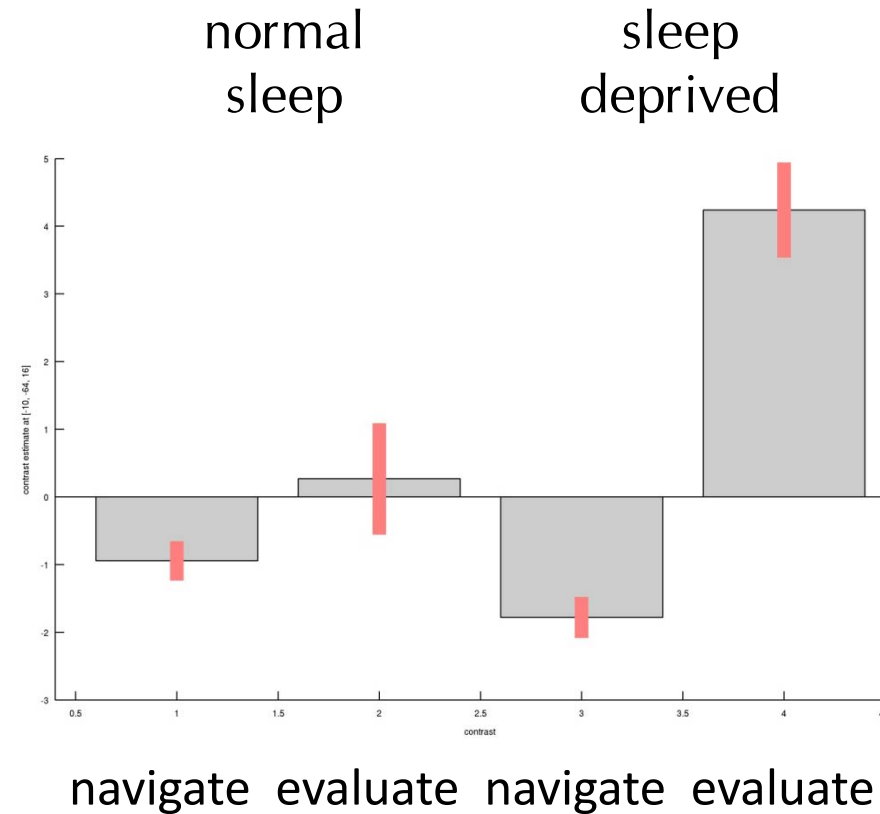
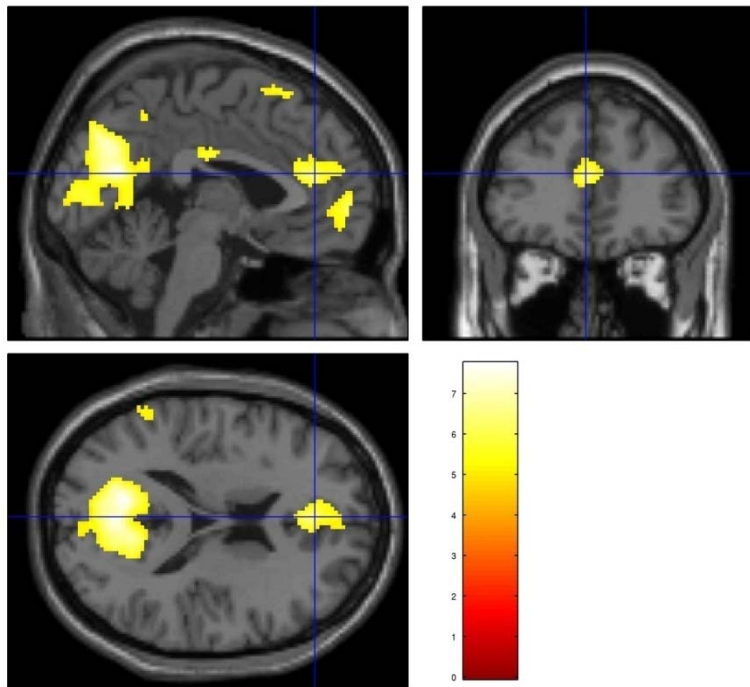
$t > 4.92$ $p < 0.05$ FWE corrected

Posterior cingulate cortex



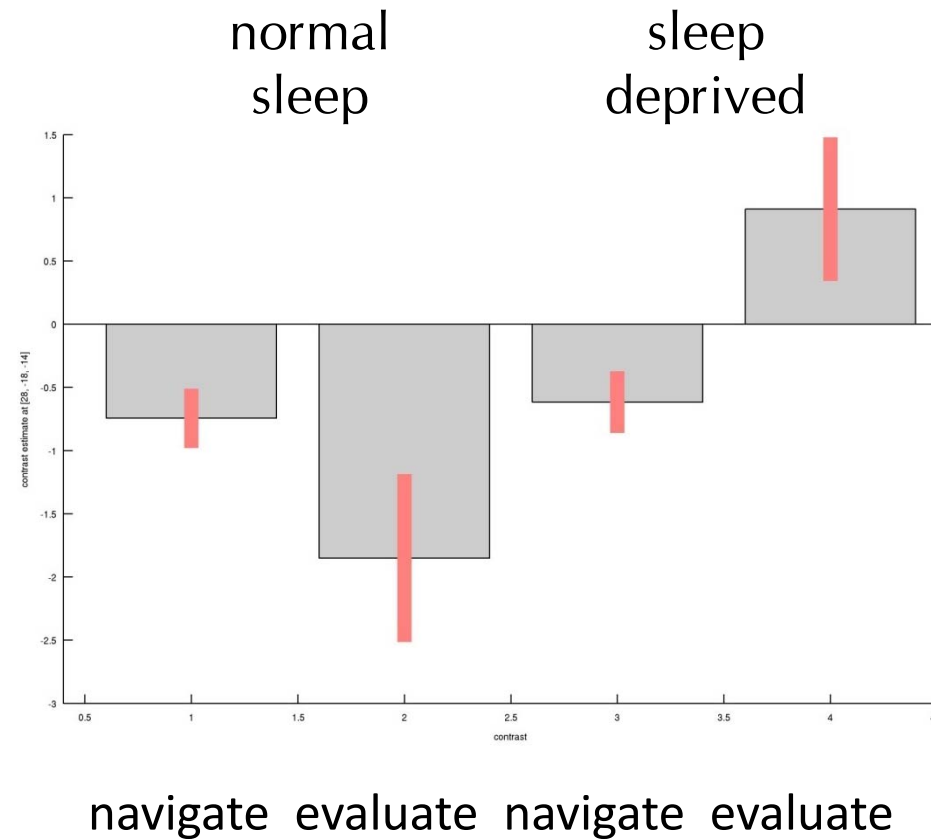
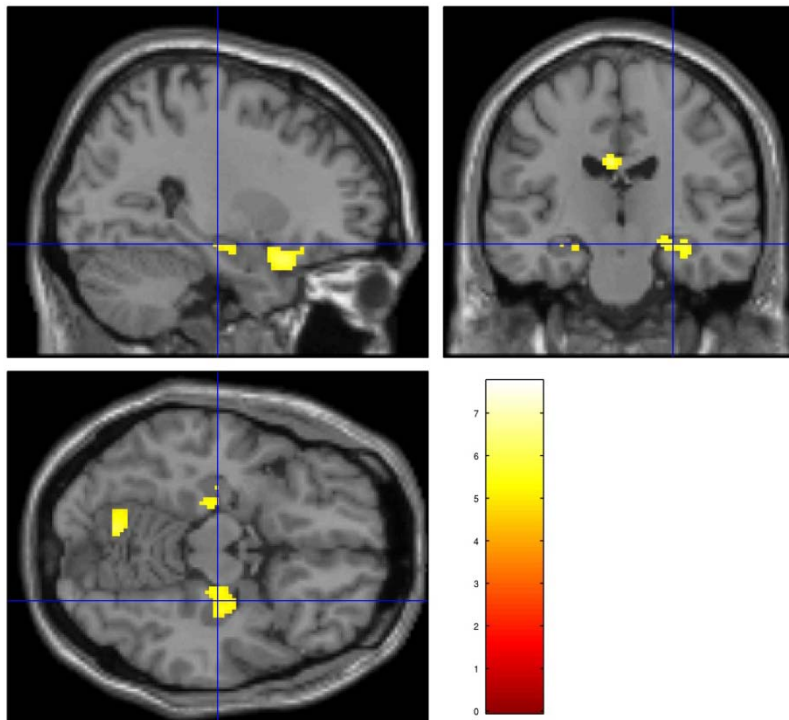
$t > 4.92$ $p < 0.05$ FWE corrected

Medial prefrontal cortex

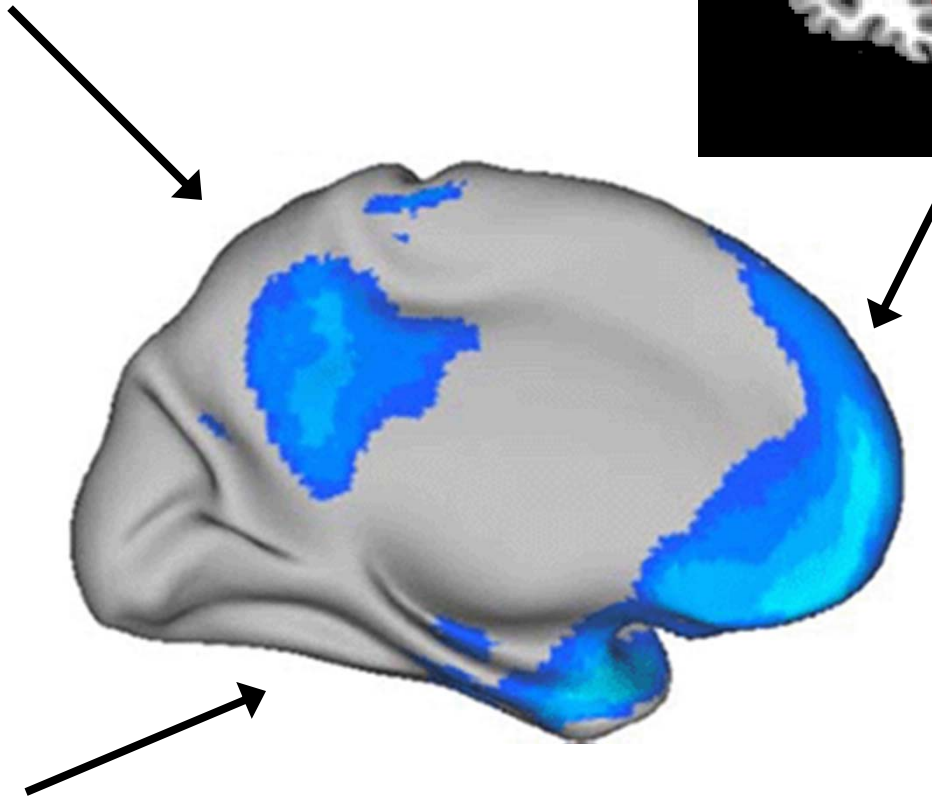
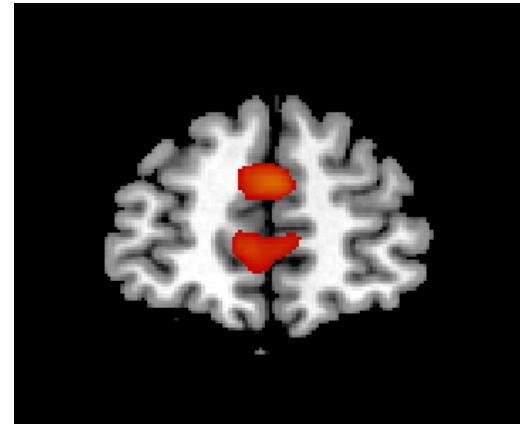


$t > 4.92$ $p < 0.05$ FWE corrected

Right hippocampus

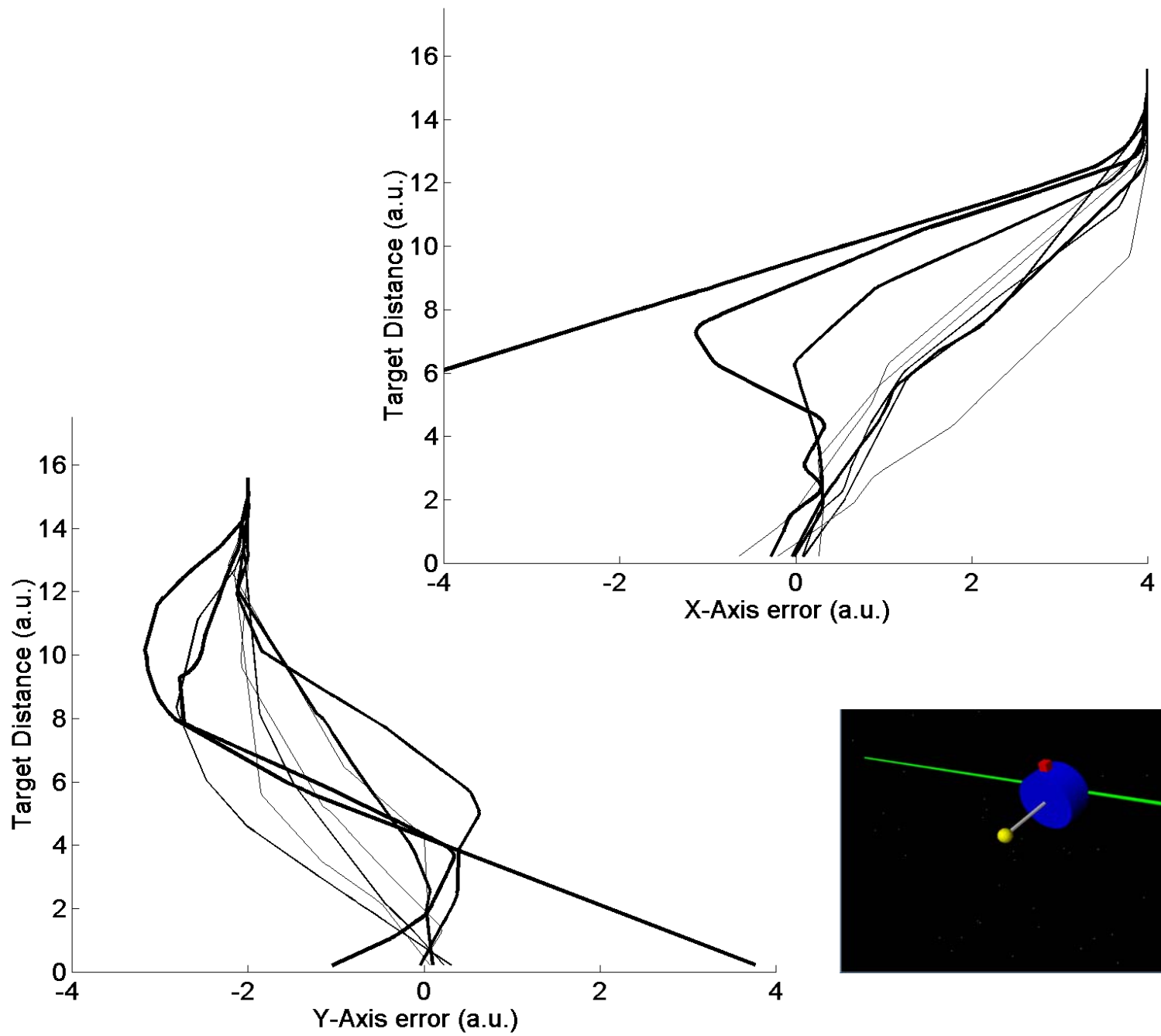


$t > 4.92$ $p < 0.05$ FWE corrected



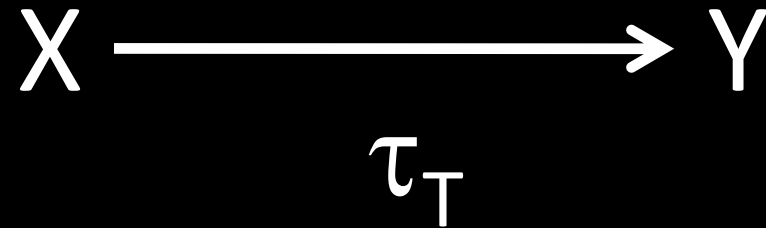
Default network from Buckner NYAS 2008

Can brain activity measured while engaged in a demanding task predict performance better than behavioral measures alone?

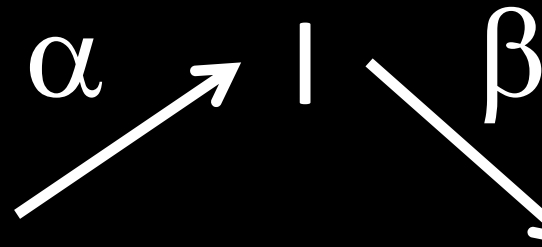


What is mediation?

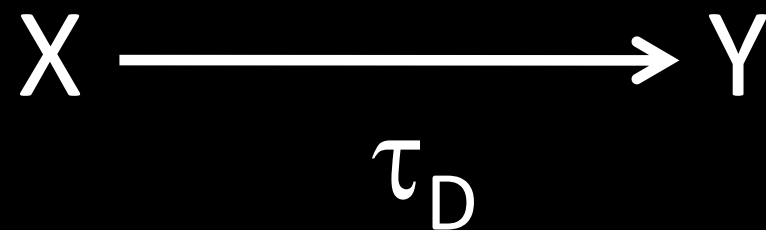
Total effect



Indirect effect



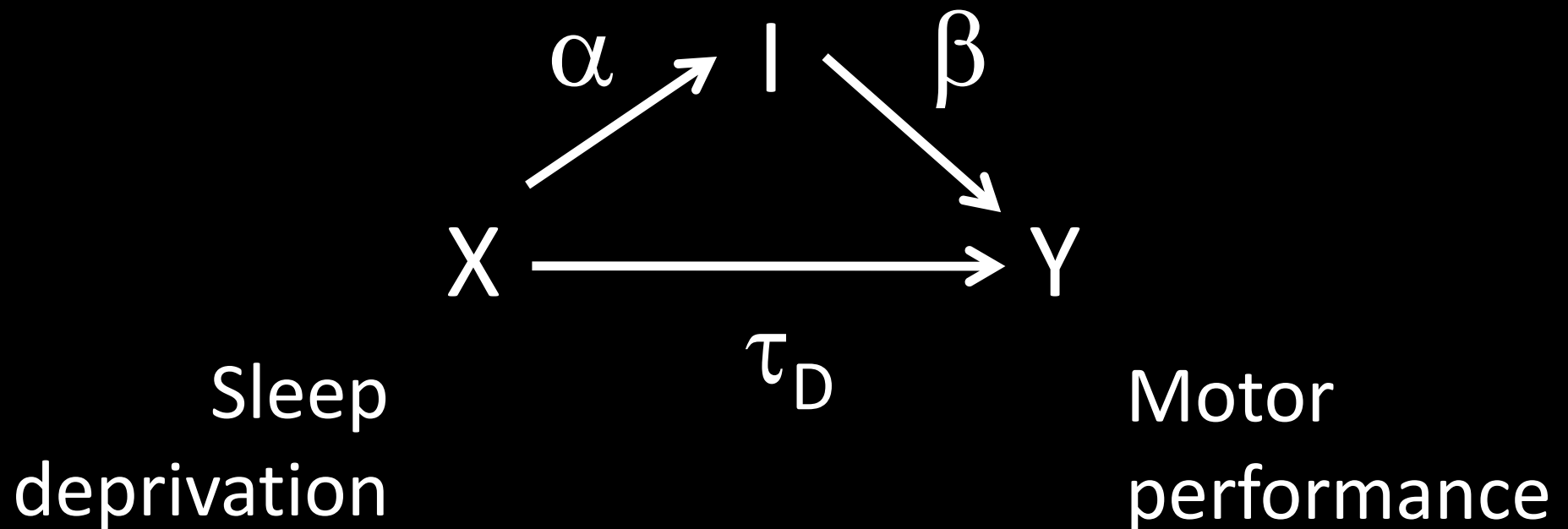
Direct effect



Mediation is a causal model

Can brain activity predict motor performance?

Regional neural activity

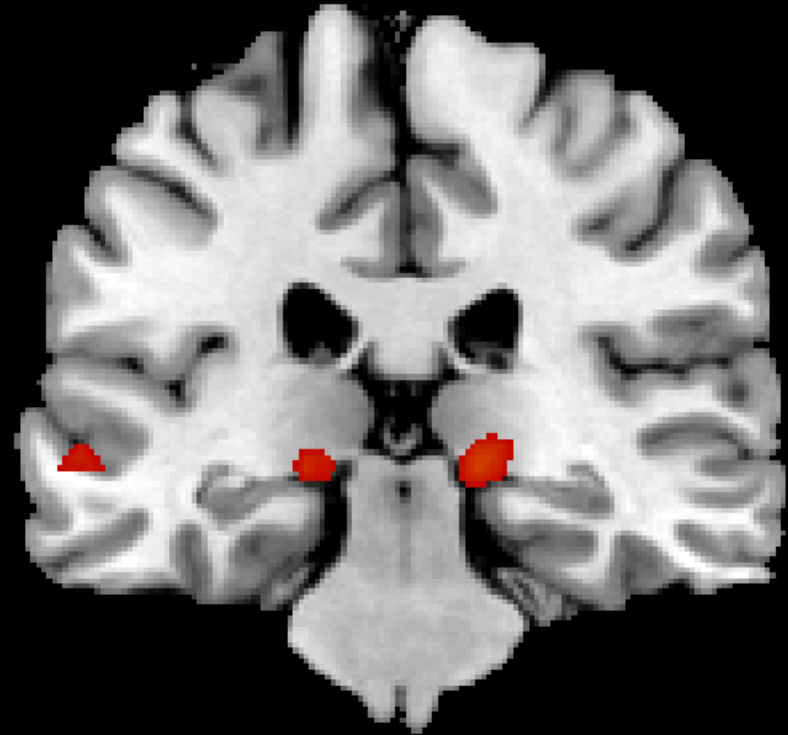
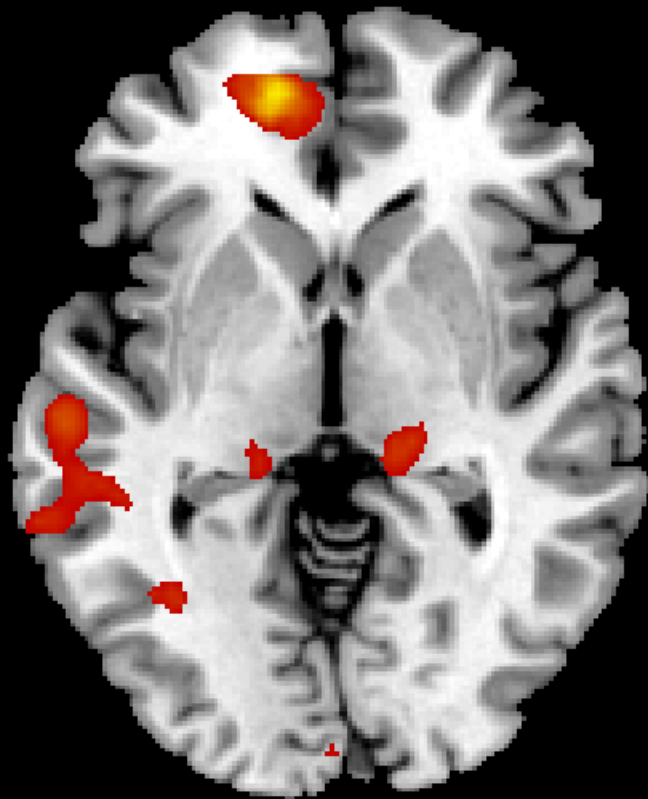


Occipital brain activity during NAVIGATION predicts motor performance better than the degree of sleep deprivation

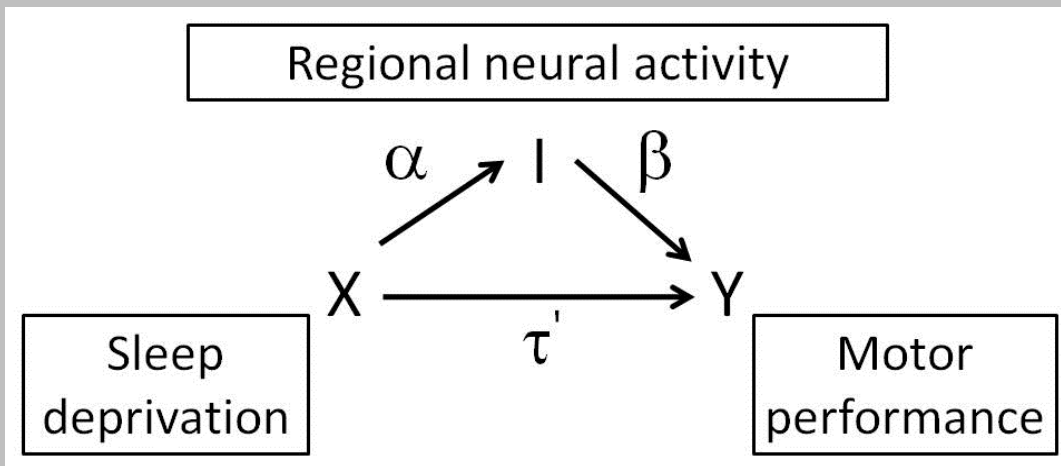
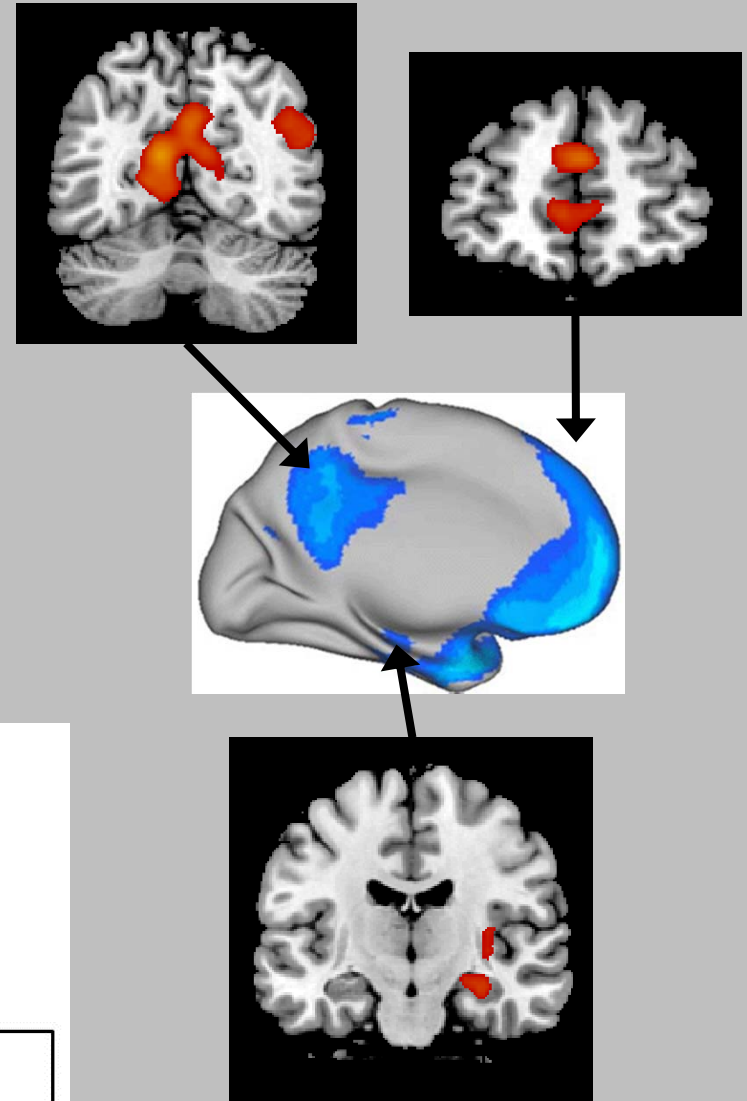
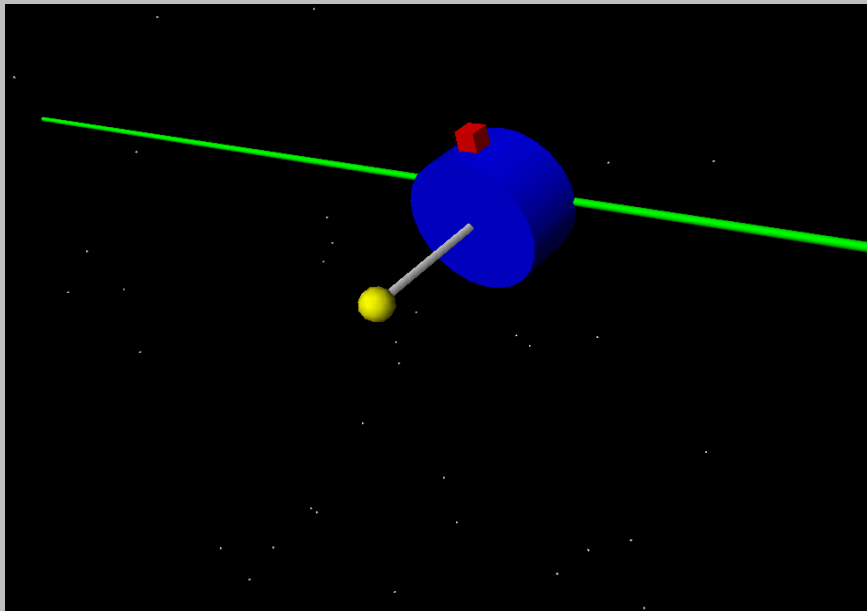


Sobel Test $z > 1.5$

Thalamic and prefrontal activity during
EVALUATION predict motor performance
better than the degree of sleep deprivation



Sobel Test $z > 1.5$



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Structural Equation Modelling (SEM)

- Another way of measuring effective connectivity
- Like PPI, looks at how effective connectivity is affected by experimental variables
- PET or fMRI

- Looks at covariances in activity between different brain areas (the degree to which their activity is related).
- Combines these data with anatomical model of how the areas are connected to one another
- Connectivity can be compared over time, or across different conditions (eg different levels of attention)

Steps in SEM

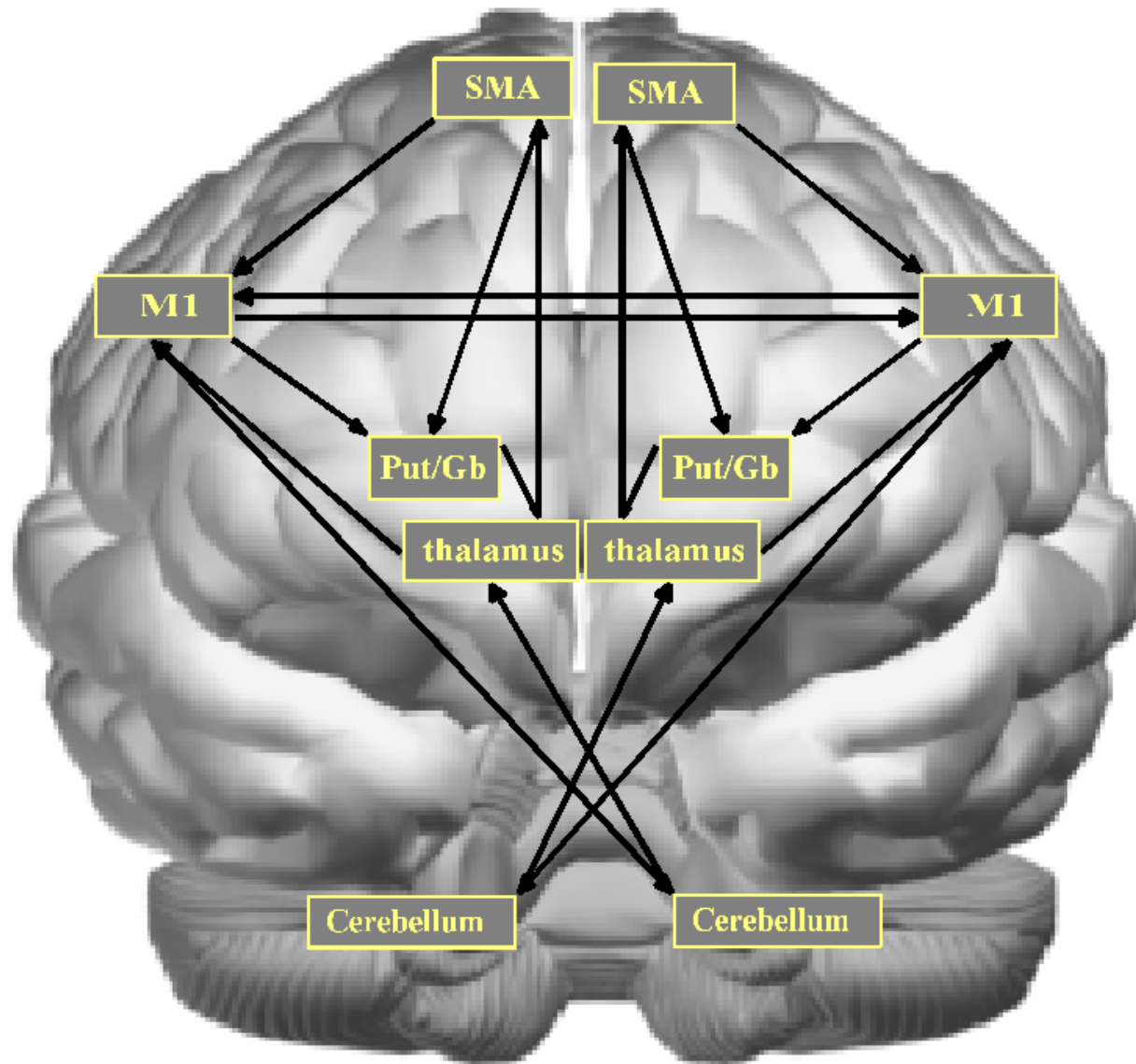
1. Select regions of interest
2. Build model specifying how they are connected to one another. Free parameters of model are 'path coefficients' – represent strength of connections
3. See what patterns of covariance this model predicts
4. Compare to observed patterns of covariance
5. 'goodness of fit' of model is diff between predicted and observed patterns

Deciding on regions

- Use existing fMRI and lesion data to identify likely areas
- We know how these areas are likely to be connected from
 - Tracer studies in animals
 - Diffusion Tensor Imaging (DTI) studies in humans

Advantages and Disadvantages

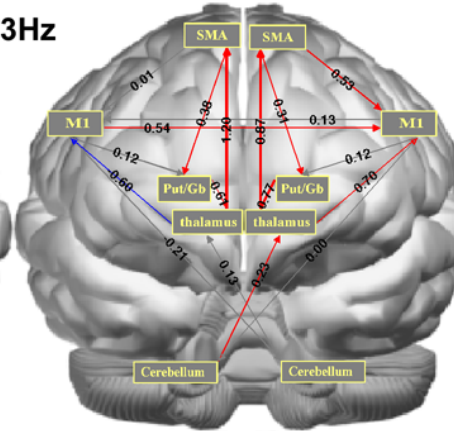
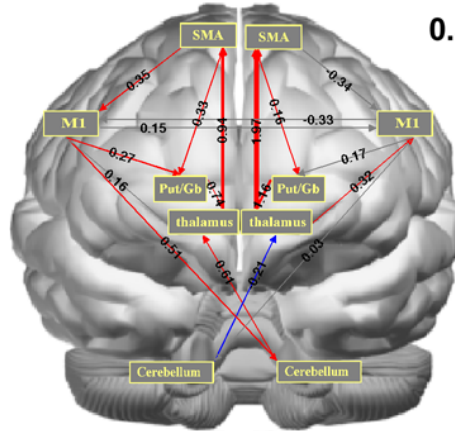
- Unlike PPI, it is possible to examine the influence of many brain areas simultaneously
- But the models do not allow the strength of a connection to vary over the time series



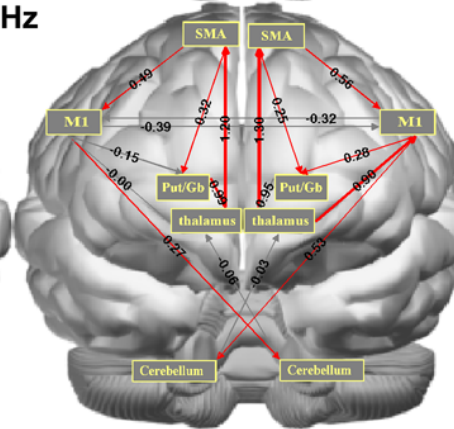
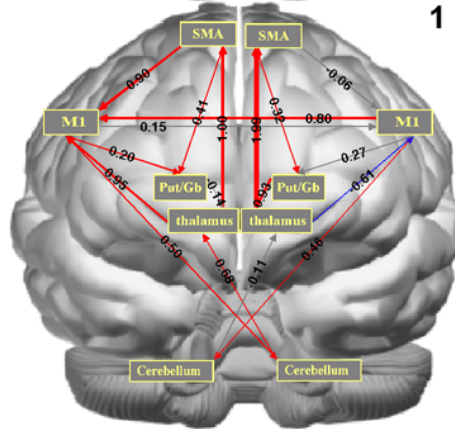
Left hand movement

Right hand movement

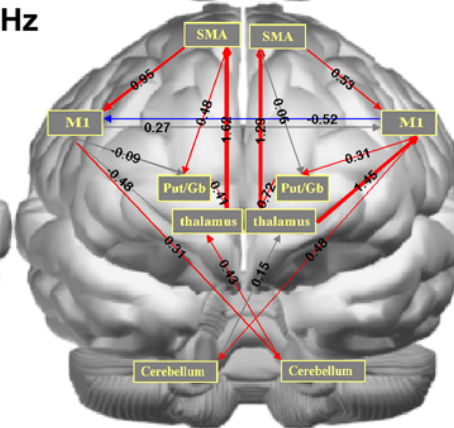
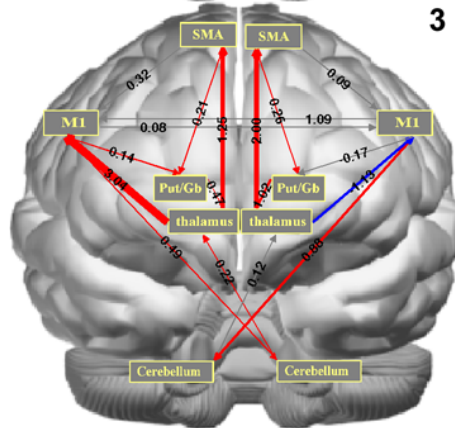
0.3Hz



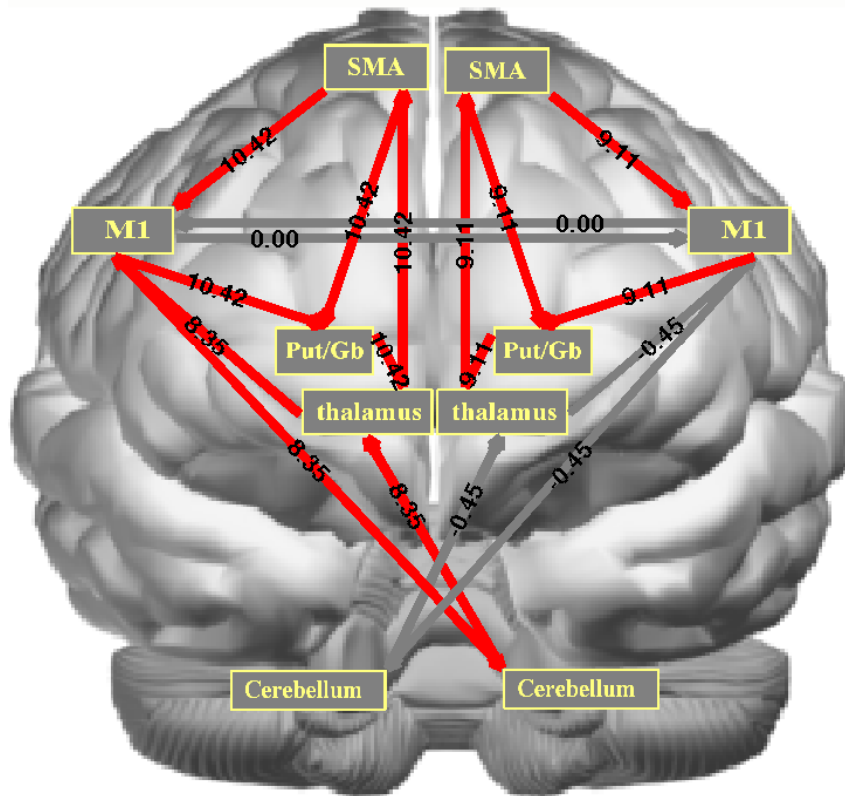
1 Hz



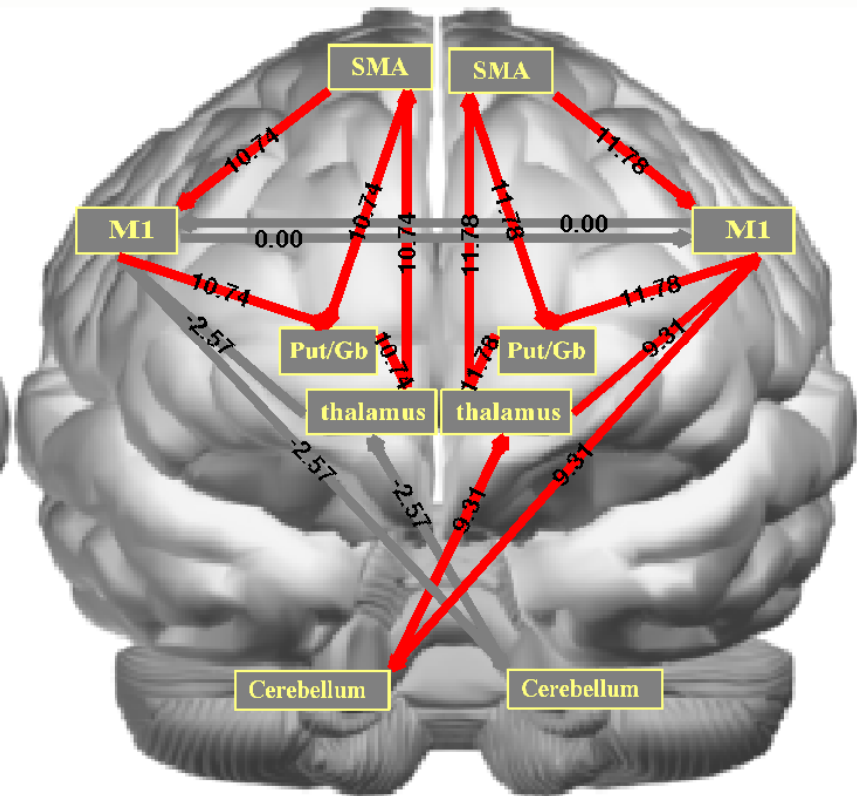
3 Hz



Left hand movement



Right hand movement



Regional Integration Modeling

- Functional connectivity
 - Bivariate correlation
 - Multivariate modeling (PCA, ICA, PLS)
- Effective connectivity
 - Psychophysiological interaction (PPI)
 - Mediation analysis
 - Structural equation modeling (SEM)
 - Multivariate autoregressive modeling (Granger causality)
 - Dynamic causal modeling (DCM)

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A

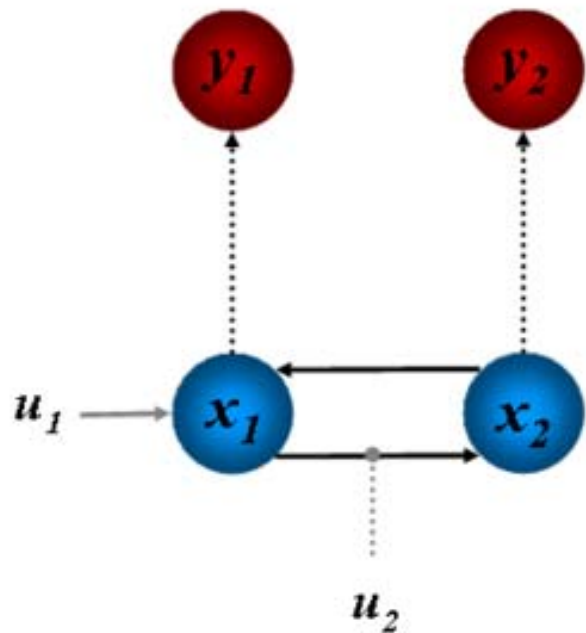
state changes *fixed connectivity* *modulation of connectivity* *input parameters*
 ↓ ↓ ↓ ↓

General bilinear state equation

$$\dot{x} = \left(A + \sum_{j=1}^m u_j B^j \right) x + C u$$

↙ ↘
external inputs

B



$$\dot{x}_1 = a_{11}x_1 + a_{12}x_2 + c_{11}u_1$$

$$\dot{x}_2 = a_{21}x_1 + a_{22}x_2 + b_{21}^{(2)}u_2x_1$$

Conceptual overview

Neuronal state equation $\dot{z} = F(z, u, \theta^n)$

The bilinear model $\dot{z} = (A + \sum u_j B^j)z + Cu$

effective connectivity

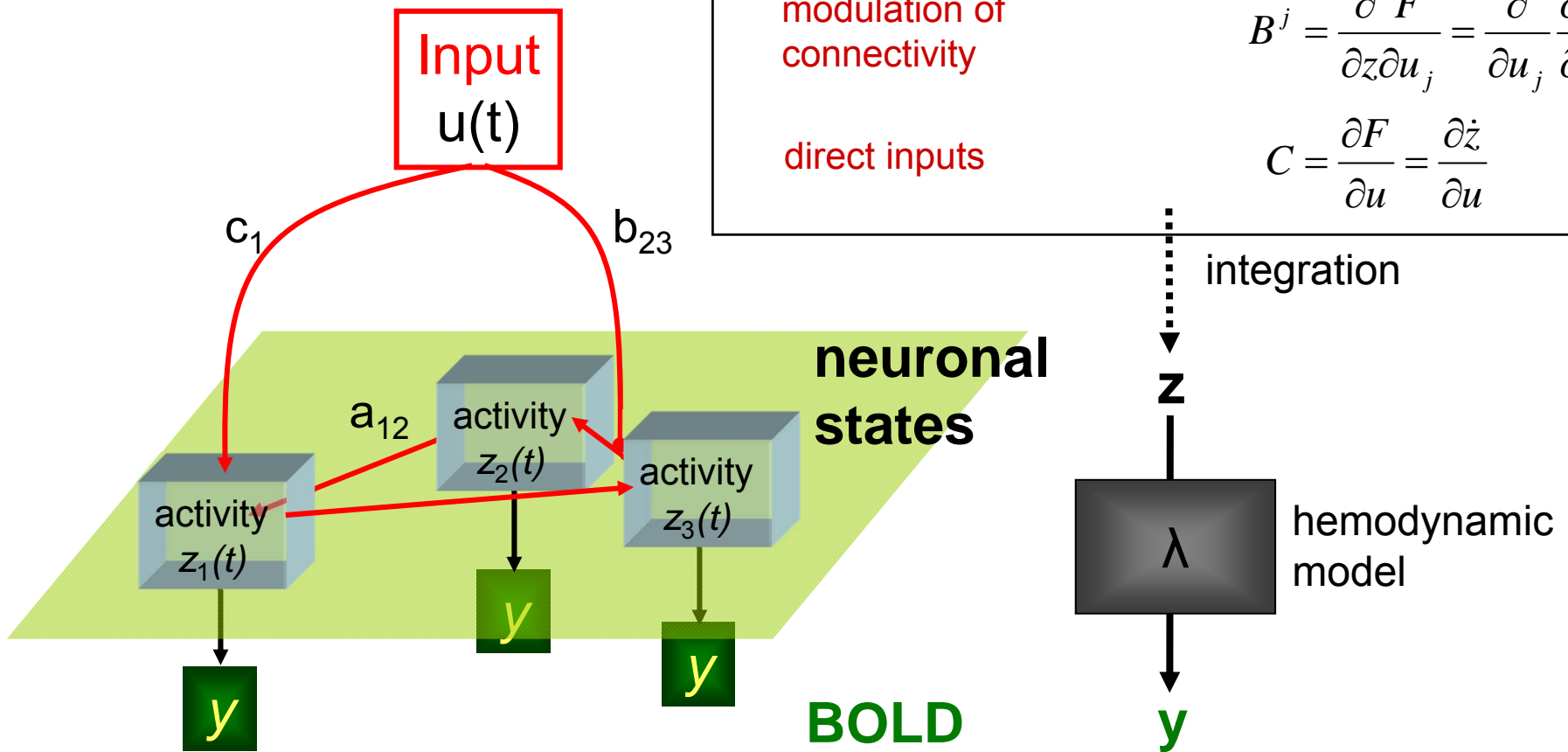
modulation of connectivity

direct inputs

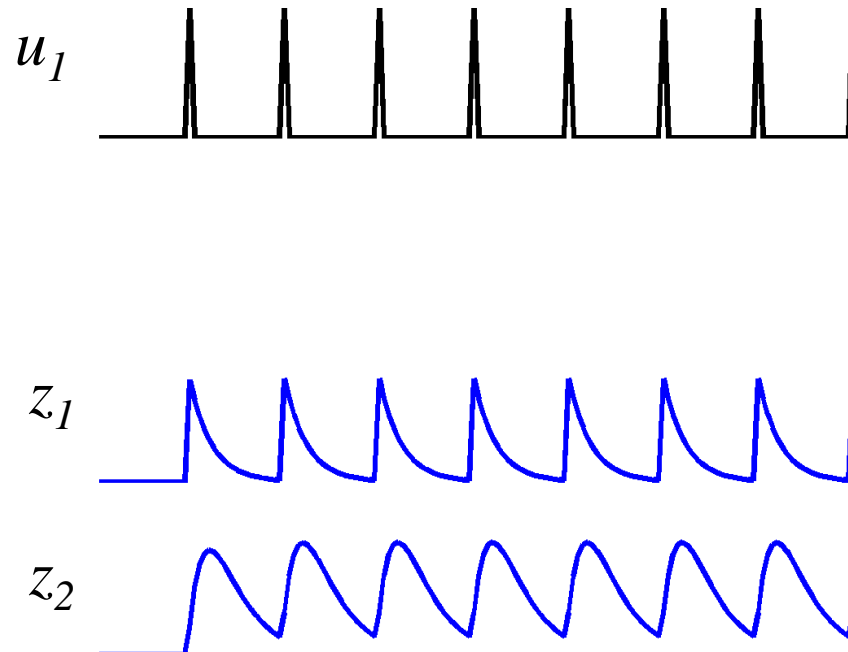
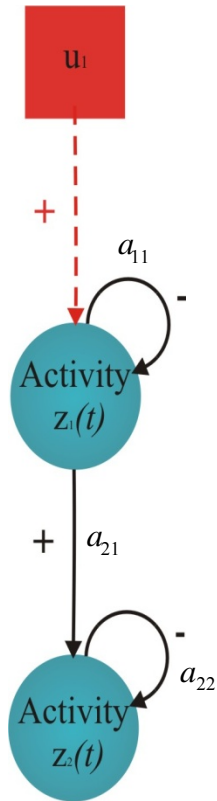
$$A = \frac{\partial F}{\partial z} = \frac{\partial \dot{z}}{\partial z}$$

$$B^j = \frac{\partial^2 F}{\partial z \partial u_j} = \frac{\partial}{\partial u_j} \frac{\partial \dot{z}}{\partial z}$$

$$C = \frac{\partial F}{\partial u} = \frac{\partial \dot{z}}{\partial u}$$



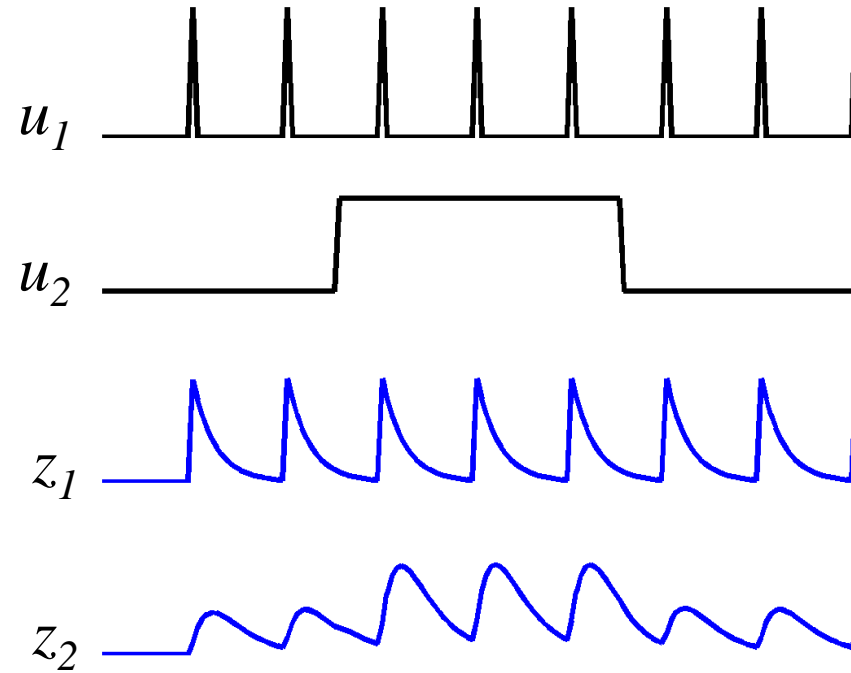
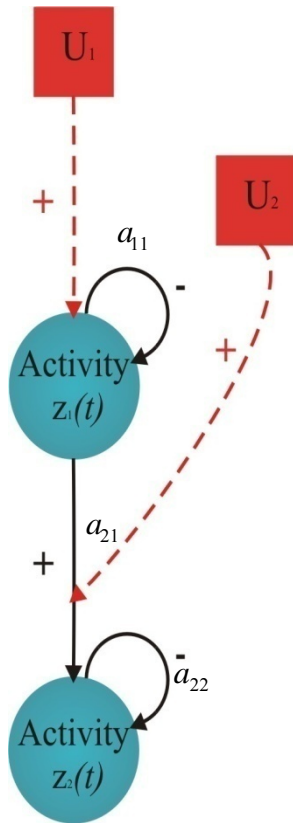
Neurodynamics: Two nodes with input



$$\begin{bmatrix} \dot{z}_1 \\ \dot{z}_2 \end{bmatrix} = \begin{bmatrix} a_{11} & 0 \\ a_{21} & a_{22} \end{bmatrix} \begin{bmatrix} z_1 \\ z_2 \end{bmatrix} + \begin{bmatrix} c \\ 0 \end{bmatrix} u_1 \quad a_{21} > 0$$

activity in z_2 is coupled to z_1 via coefficient a_{21}

Neurodynamics: positive modulation

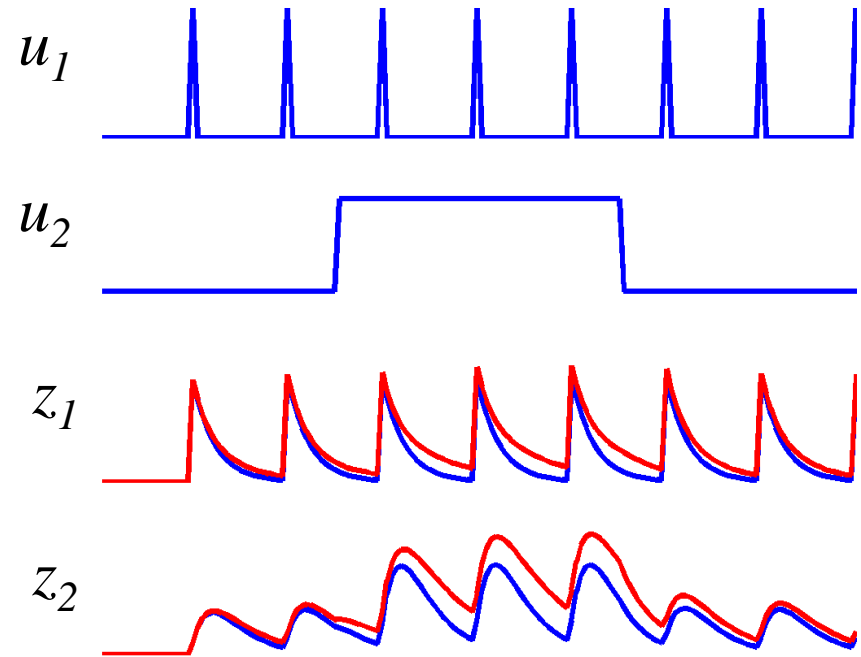
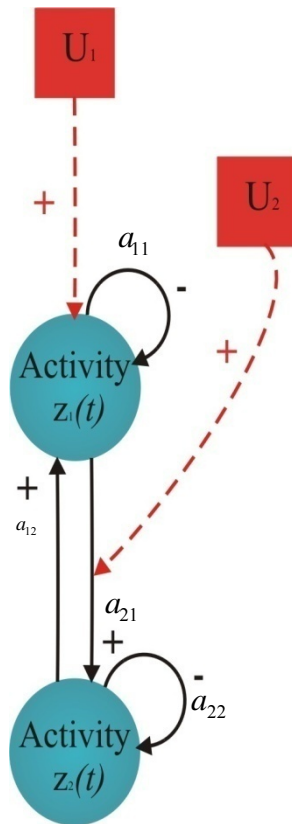


$$\begin{bmatrix} \dot{z}_1 \\ \dot{z}_2 \end{bmatrix} = \begin{bmatrix} a_{11} & 0 \\ a_{21} & a_{22} \end{bmatrix} \begin{bmatrix} z_1 \\ z_2 \end{bmatrix} + u_2 \begin{bmatrix} 0 \\ b_{21}^2 \end{bmatrix} + \begin{bmatrix} c \\ 0 \end{bmatrix} u_1$$

modulatory input u_2 activity through
the coupling a_{21}

$$b_{21}^2 > 0$$

Neurodynamics: reciprocal connections



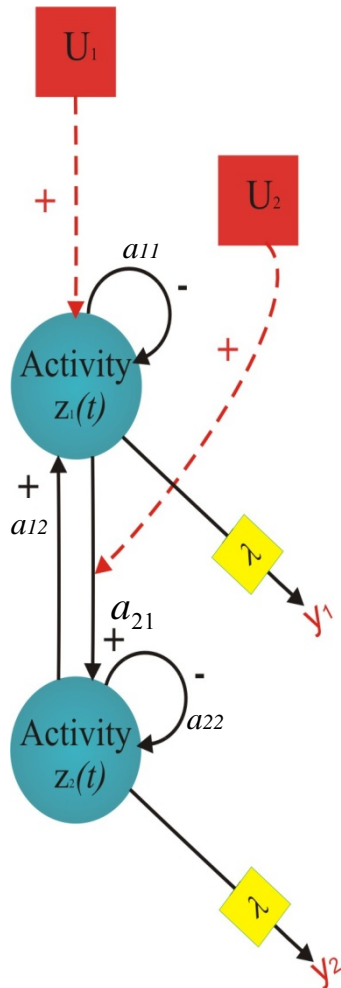
$$\begin{bmatrix} \dot{z}_1 \\ \dot{z}_2 \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} \begin{bmatrix} z_1 \\ z_2 \end{bmatrix} + u_2 \begin{bmatrix} 0 \\ b_{21}^2 \end{bmatrix} + \begin{bmatrix} c \\ 0 \end{bmatrix} u_1$$

$$a_{21} > 0 \quad a_{12} > 0 \quad b_{21}^2 > 0$$

reciprocal
connection
disclosed by

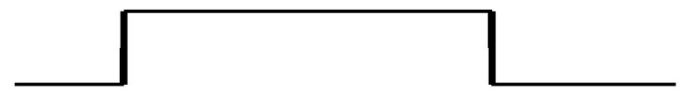
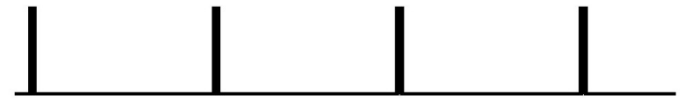
u_2

Hemodynamics: reciprocal connections

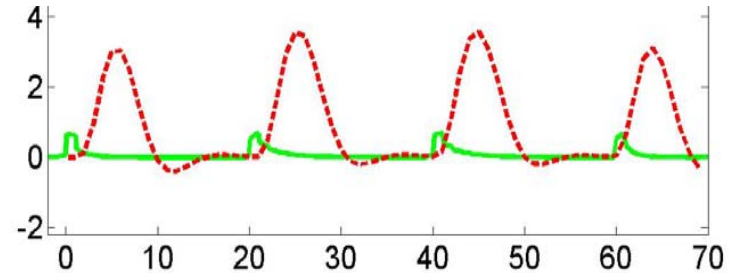


$$\begin{bmatrix} \dot{z}_1 \\ \dot{z}_2 \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} \begin{bmatrix} z_1 \\ z_2 \end{bmatrix} + u_2 \begin{bmatrix} 0 & 0 \\ b_{21}^2 & 0 \end{bmatrix} \begin{bmatrix} z_1 \\ z_2 \end{bmatrix} + \begin{bmatrix} c \\ 0 \end{bmatrix} u_1$$

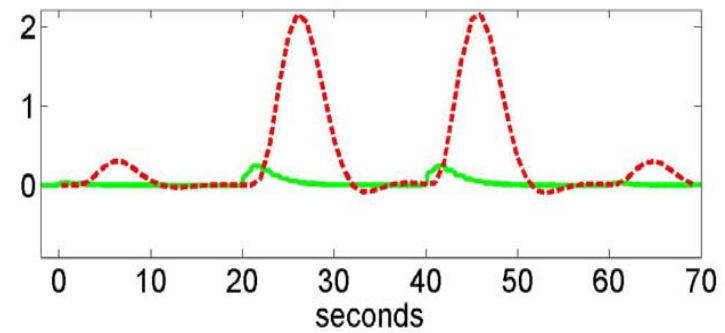
$a_{21} > 0 \quad a_{12} > 0 \quad b_{21}^2 > 0$



Bold Response



Bold Response



green: neuronal activity
red: bold response

Conceptual overview

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effective connectivity

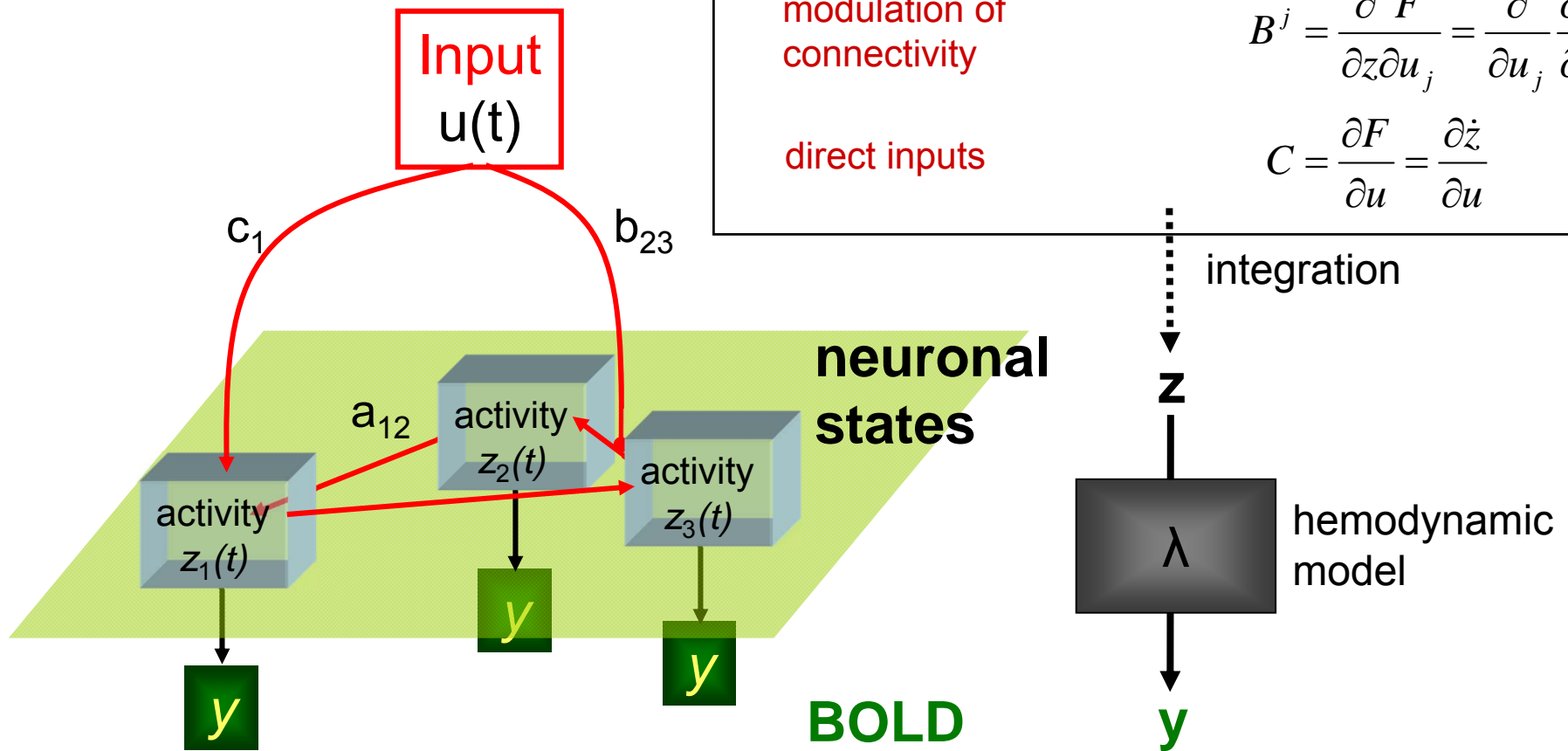
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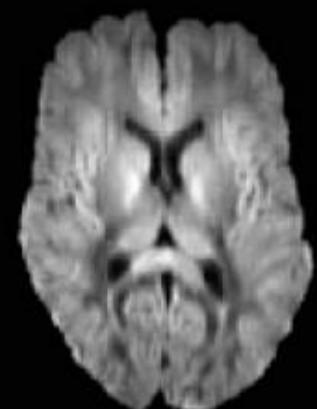
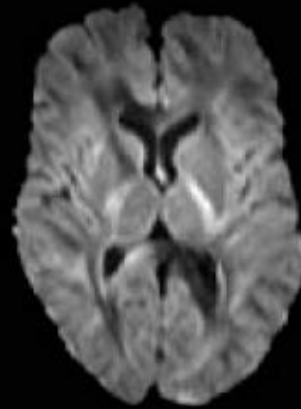
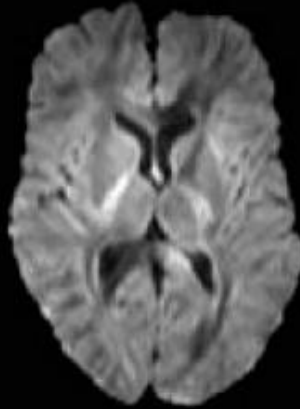
- SPM 8/12
- ART Toolbox
- PPI
- GIFT
- DCM
- Connectivity Toolbox
- Brainwaver



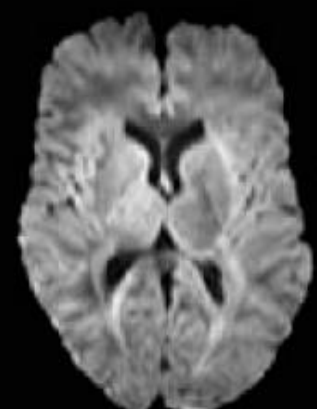
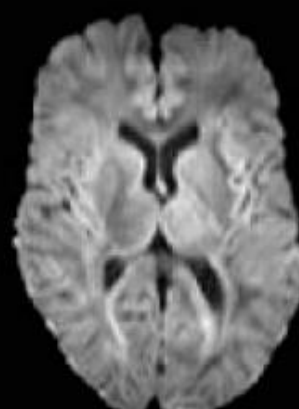
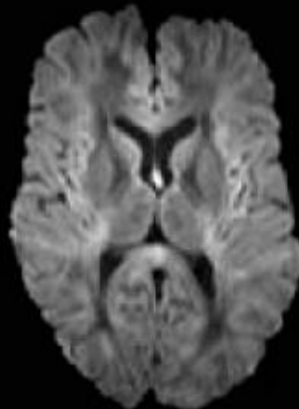


Diffusion Tensor Imaging

- Diffusion sensitive gradients applied in six directions with $b = 800$



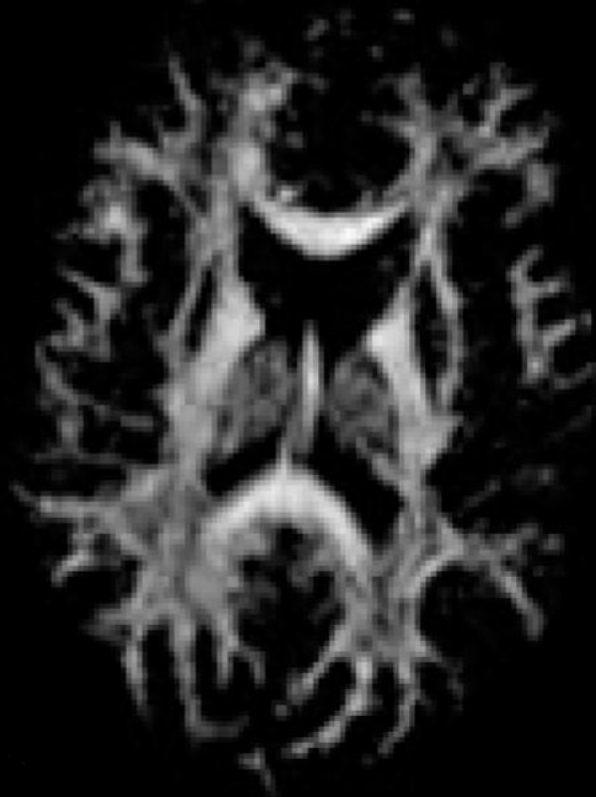
- Dark areas represent areas with a higher diffusion



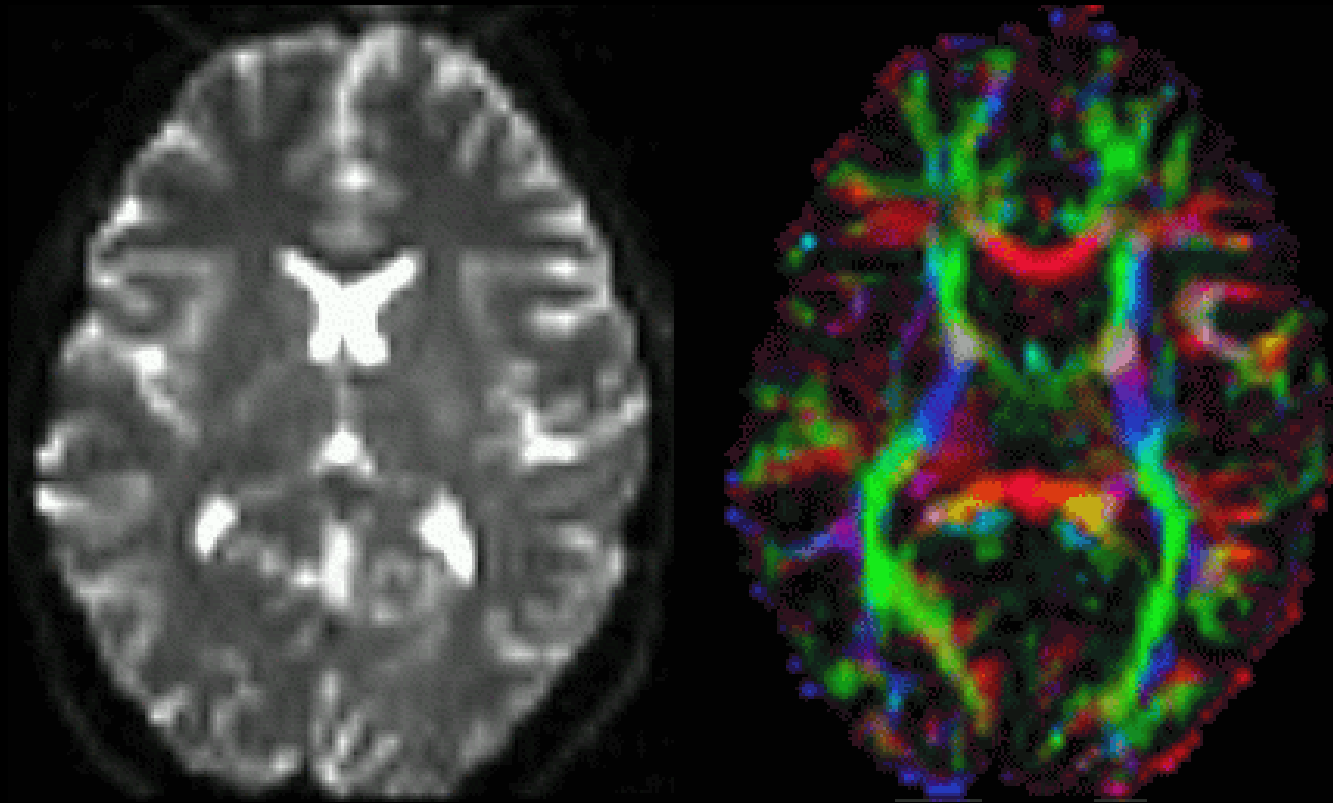
Fractional Anisotropy (FA)

- Measure of degree of anisotropy regardless of direction
- Brighter areas correspond to areas with higher FA

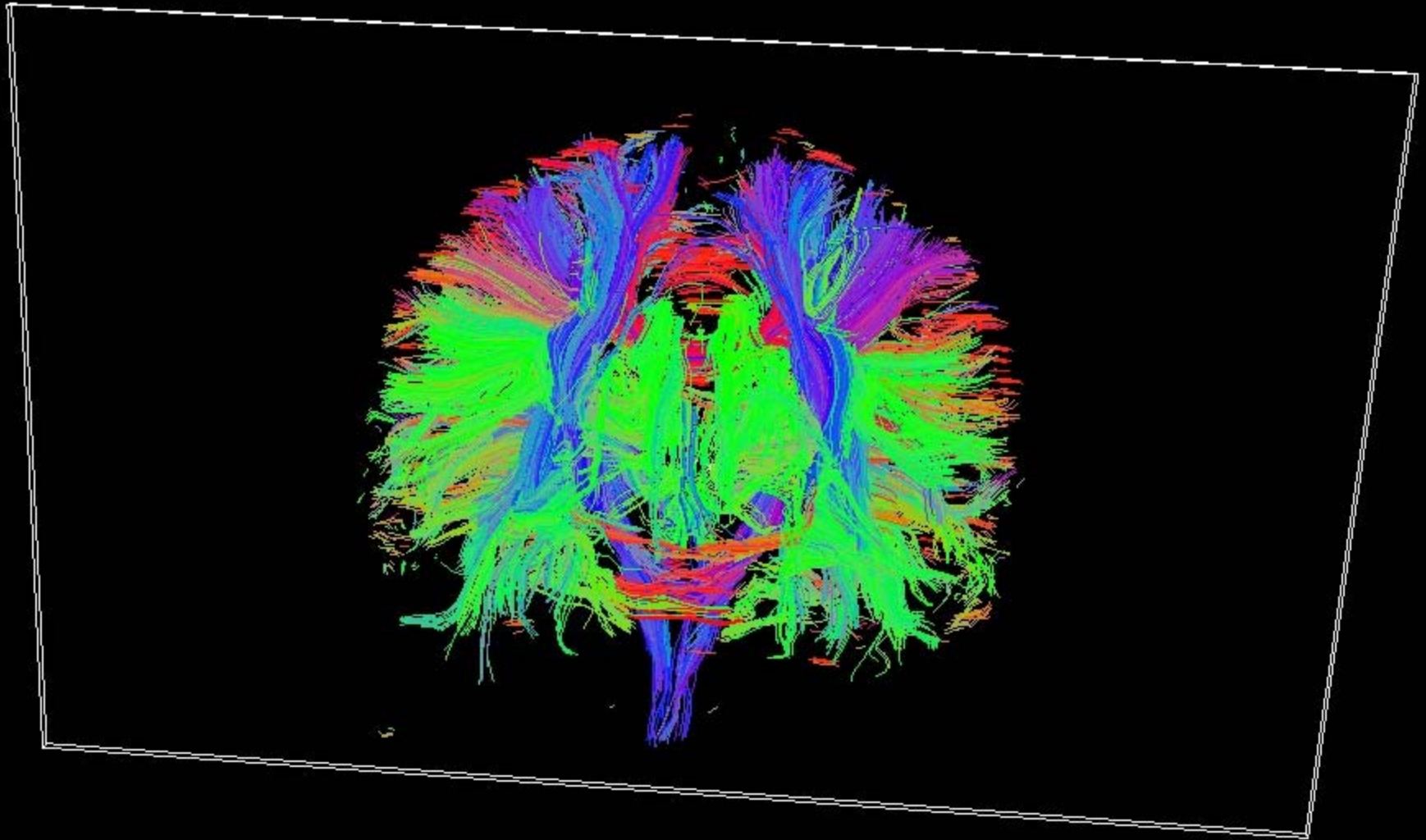
$$FA^2 = \frac{(l_x - l_y)^2 + (l_x - l_z)^2 + (l_y - l_z)^2}{2(l_x^2 + l_y^2 + l_z^2)}$$



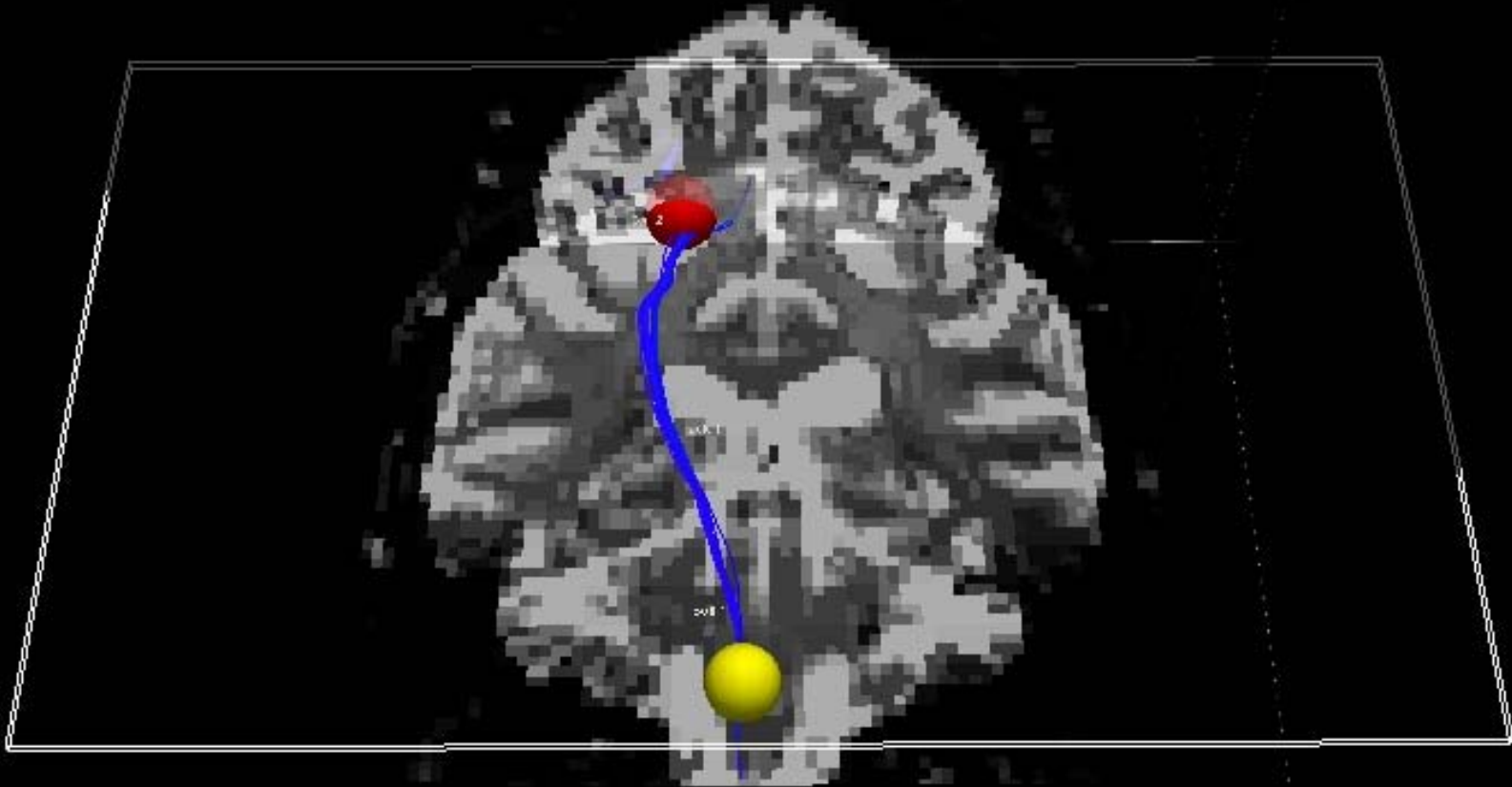
Diffusion Directions



Red = Left-Right
Green = Anterior-Posterior
Blue = Superior-Inferior



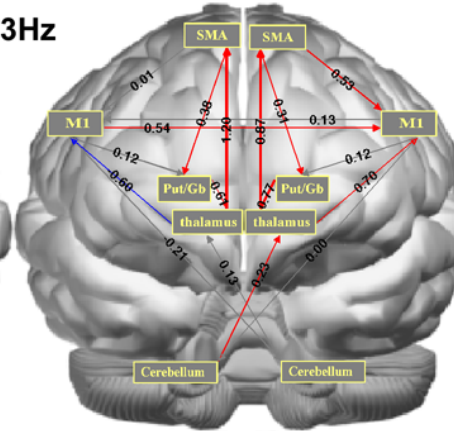
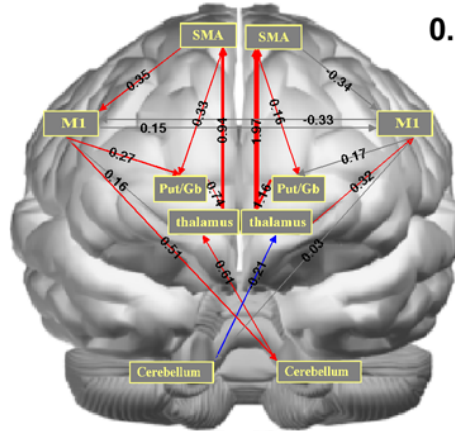
A



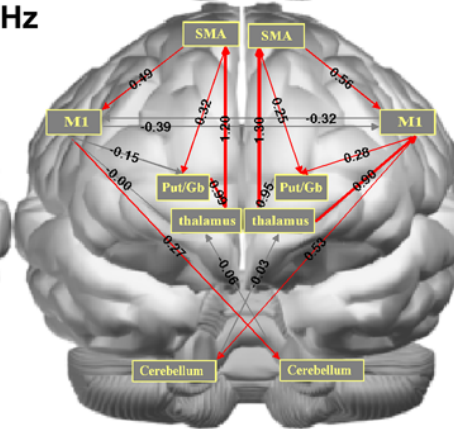
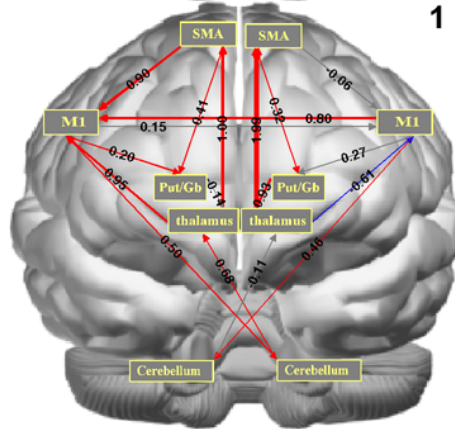
Left hand movement

Right hand movement

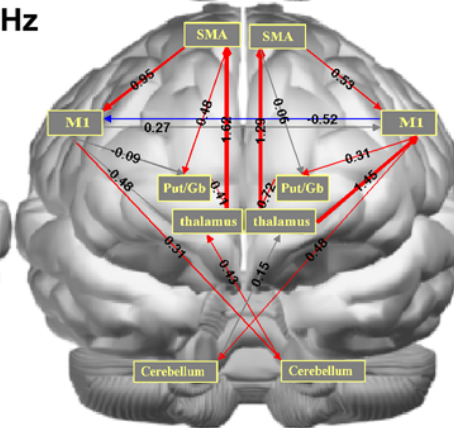
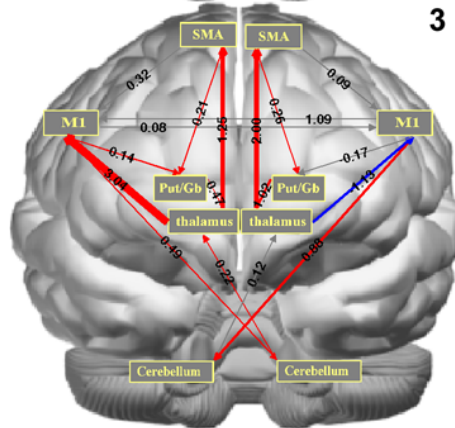
0.3Hz



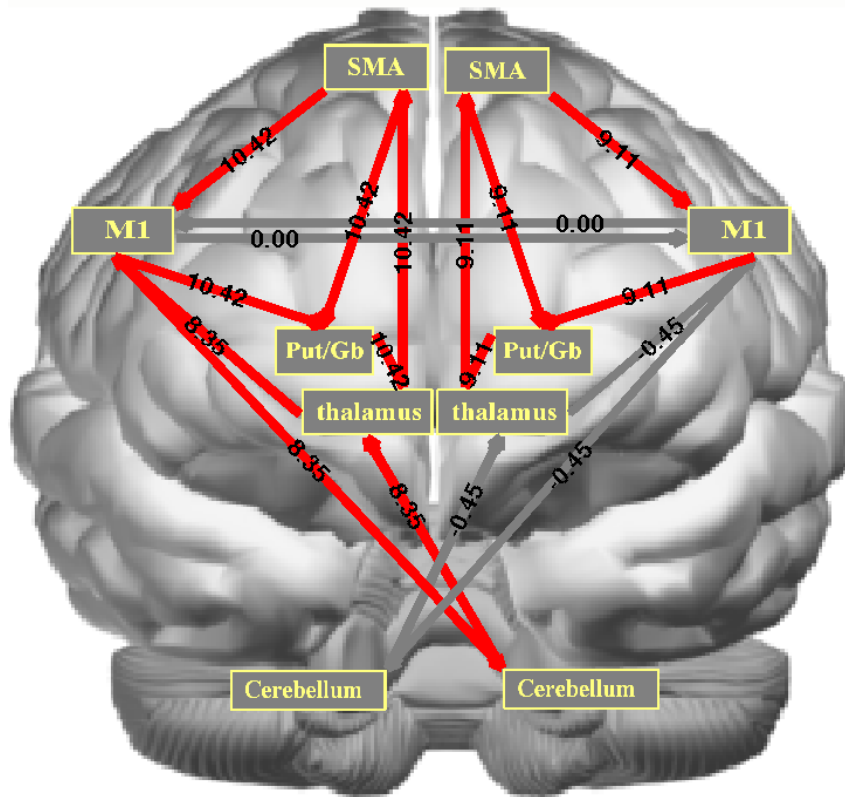
1 Hz



3 Hz



Left hand movement



Right hand movement

